

(Small-scale) Challenges to the Λ CDM Paradigm

SUT School in Astronomy and Cosmology

11 May 2024

Nicha Leethochawalit (NARIT)

(Small-scale) Challenges to the Λ CDM Paradigm

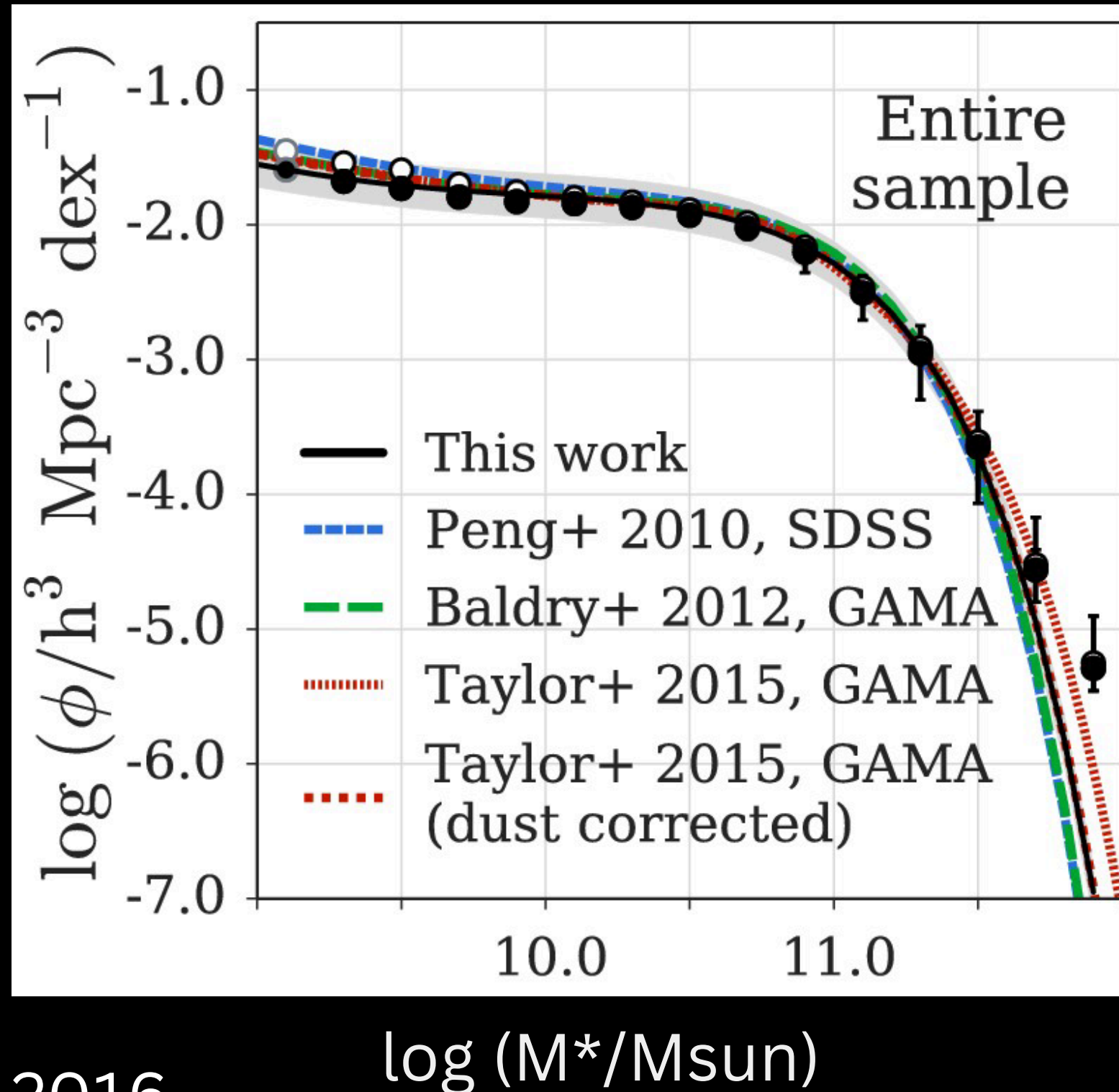
Missing Satellite

Cusp-Core Problem

Too bit too fail

Scales in galaxy- cosmology studies

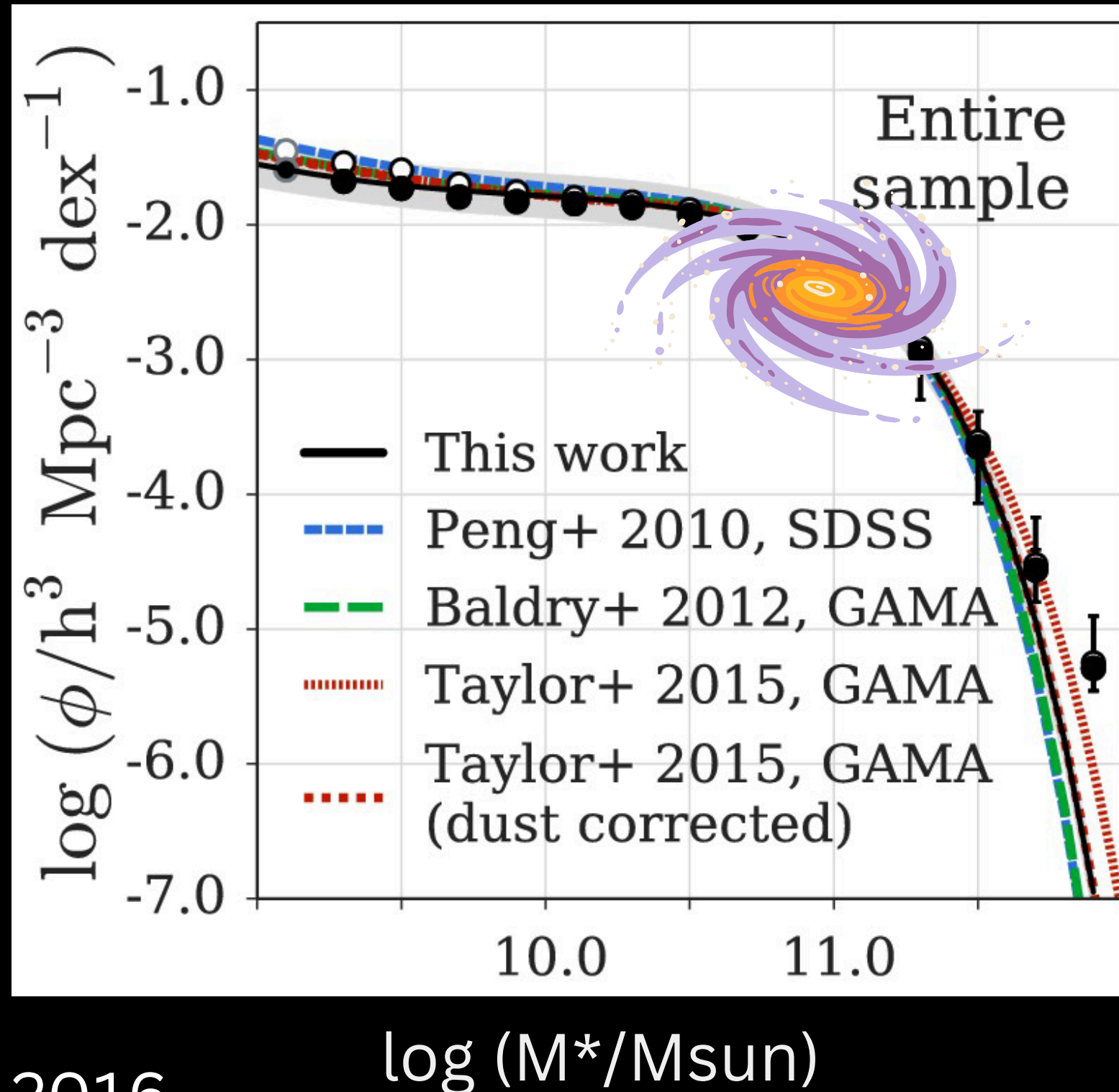
Scales in galaxy-cosmology studies: stellar mass



Typical galaxy stellar mass is
 10^6 - 10^{12} Msun

Scales in galaxy-cosmology studies: stellar mass

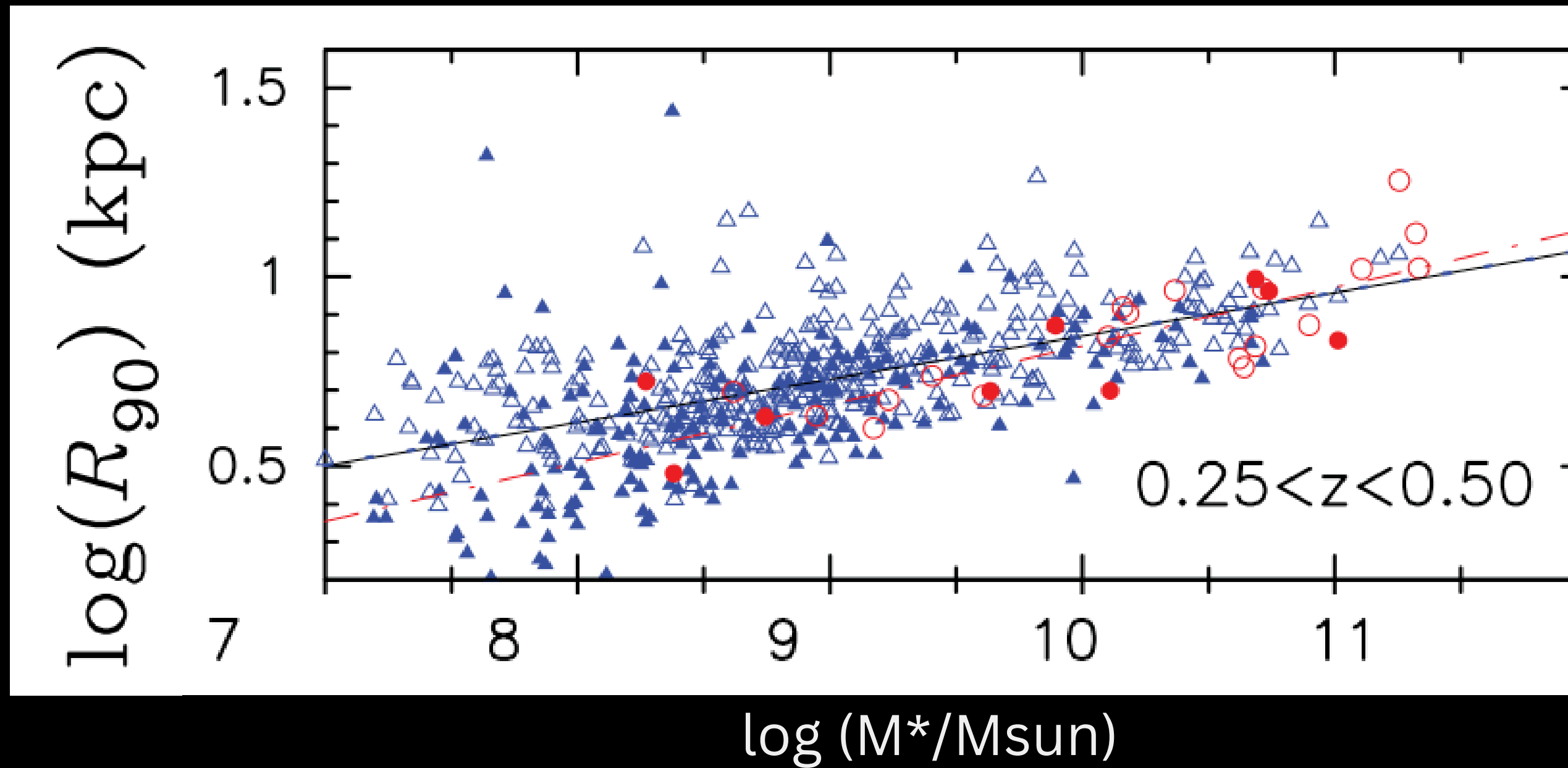
Milkyway is a typical galaxy



Typical galaxy stellar mass is
 10^6 - 10^{12} Msun

Scales in galaxy-cosmology studies: galaxy sizes

Typical galaxy size is 1-10 kpc



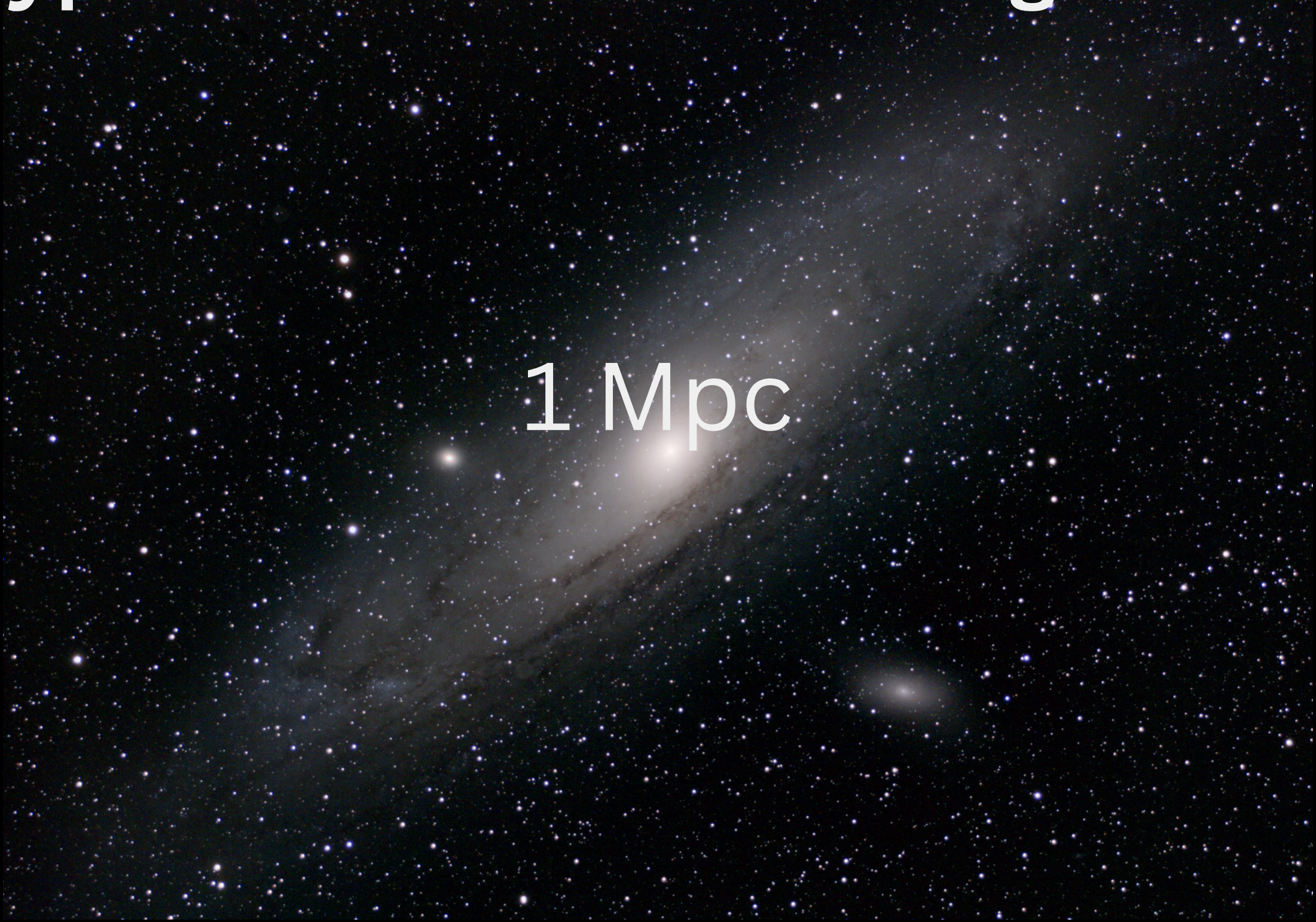
Scales in galaxy-cosmology studies

Typical distance between galaxies is



Scales in galaxy-cosmology studies

Typical distance between galaxies is



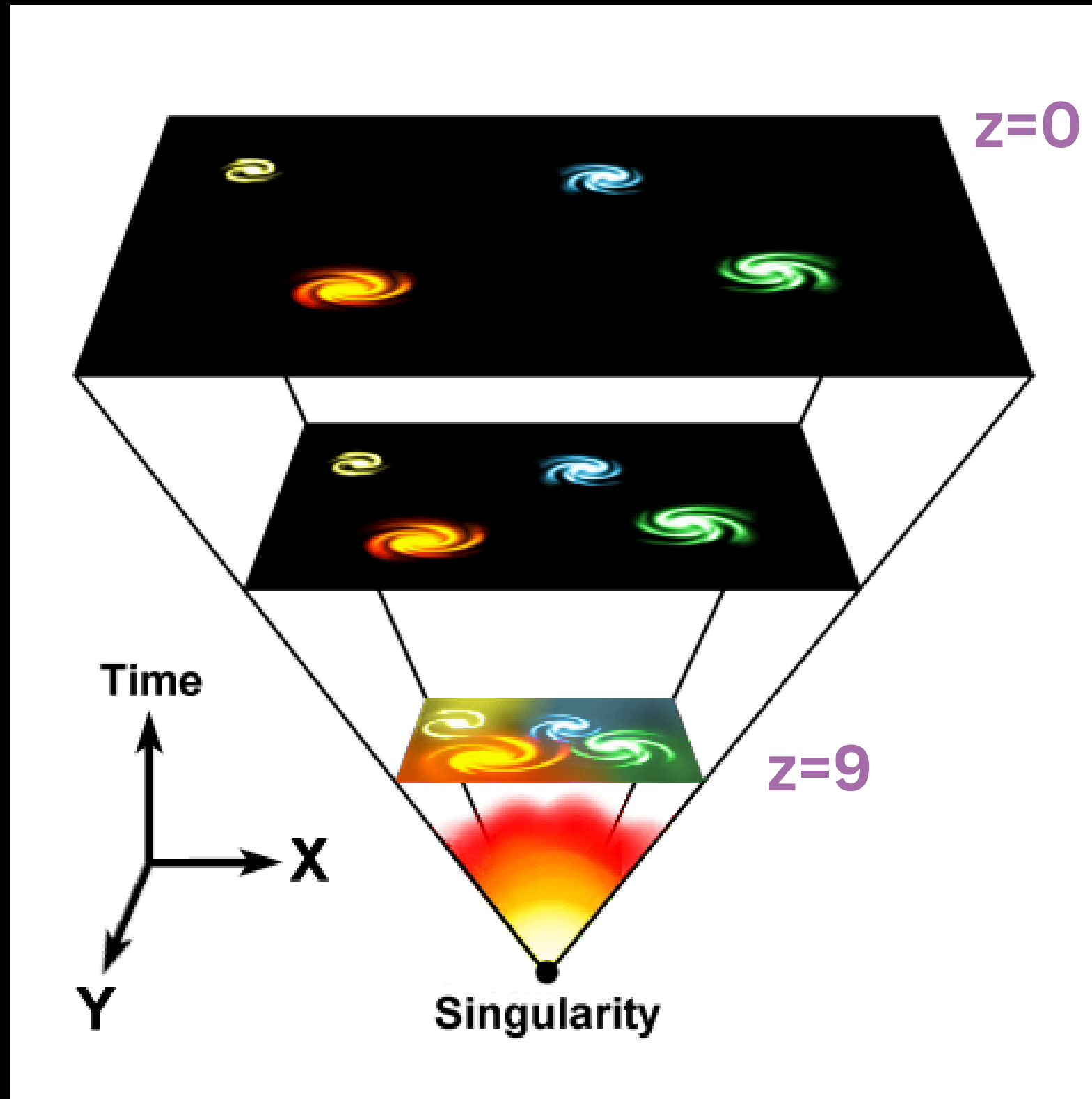
Scales in galaxy-cosmology studies: universe scale

What about size of the universe??

search: cosmology calculator

galaxy at redshift $z = 11$?

Scales in galaxy-cosmology studies: universe scale

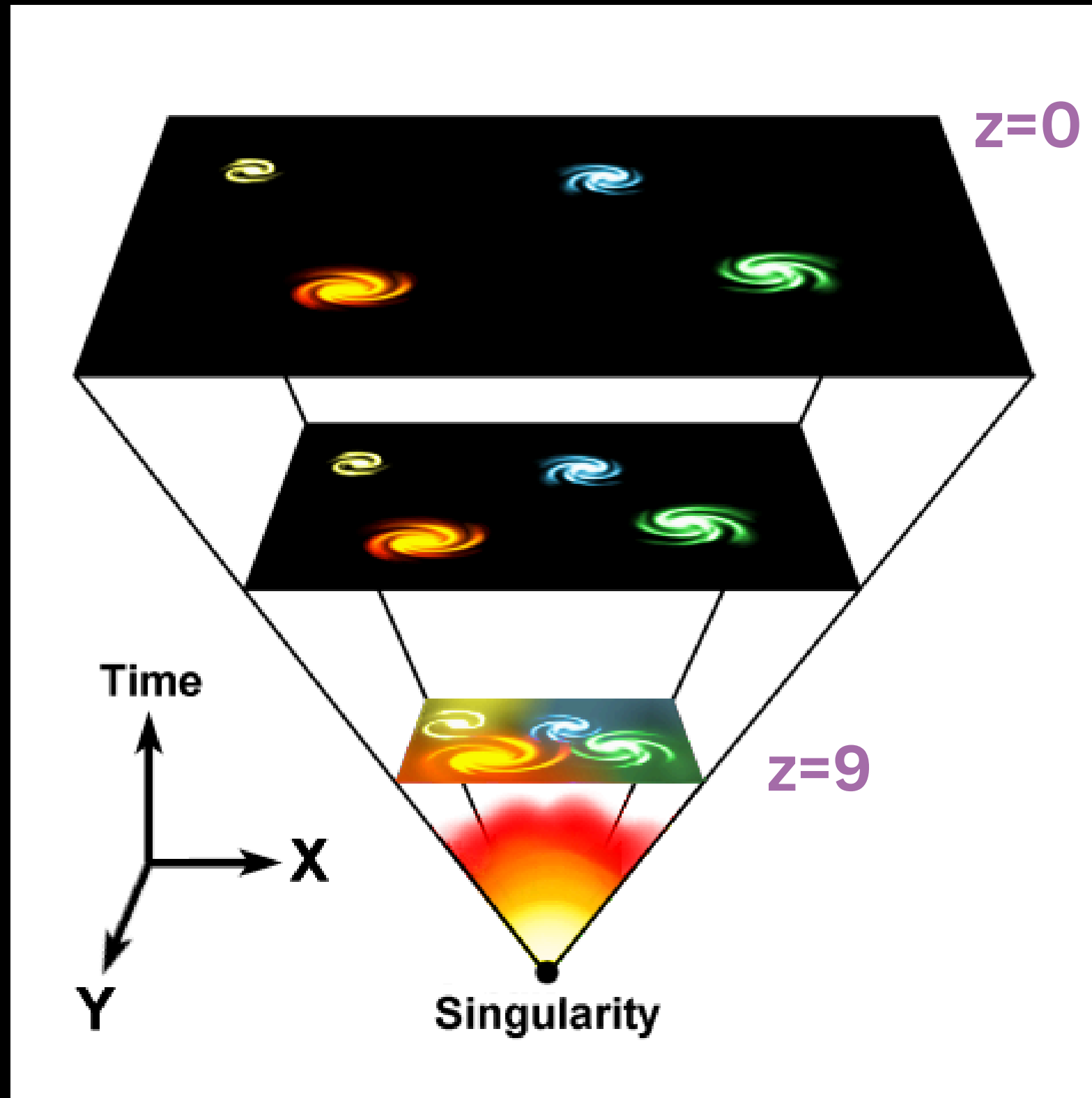


scale factor

$$a(z) \equiv 1/(1+z)$$

where $a(z=0) = 1$

Scales in galaxy-cosmology studies: universe scale



scale factor

$$a(z) \equiv 1/(1+z)$$

where $a(z=0) = 1$

Comoving distance
is 'how far we are from that galaxy if the universe were to be frozen now ($z=0$)'

Scales in galaxy-cosmology studies

So, what is the observable universe (the horizon) size in comoving scale?

Scales in galaxy-cosmology studies

So, what is the observable universe (the horizon) size in comoving scale?

~15000 Mpc in radius

Scales in galaxy-cosmology studies

Conclusion:

galaxy stellar mass: 10^6 - 10^{12} Msun

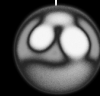
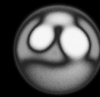
galaxy size: 1-10 kpc

distance between galaxies: 1 Mpc

Universe size: 15000 Mpc

Observations

the Universe

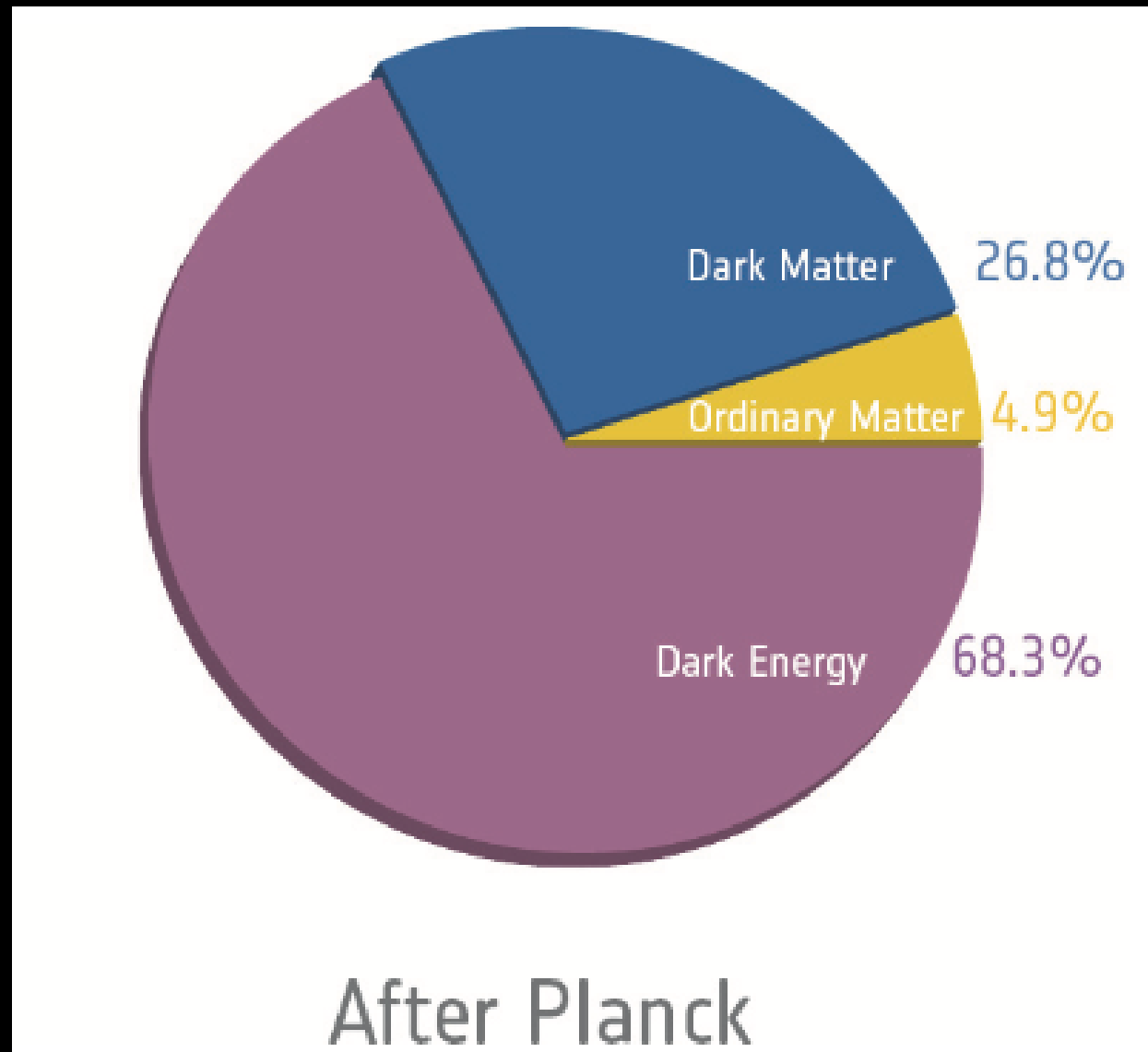


Cosmological Simulations

universes that are statistically consistent with the Universe

Cosmological Simulations

Λ CDM (Lambda cold dark matter) model - standard model of Big Bang cosmology



A universe that is dominated by cold dark matter and dark energy

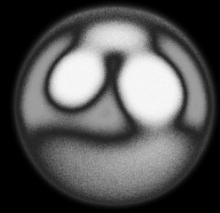
Space-time described by Friedmann equations

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3}\rho - \frac{kc^2}{3} + \frac{\Lambda c^2}{3},$$
$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3}\left(\rho + \frac{3p}{c^2}\right) + \frac{\Lambda c^2}{3},$$

With some definitions, the first eq can be written in a more familiar form:

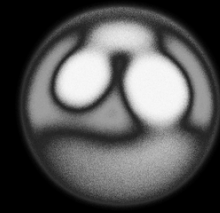
$$H(z) = H_0 \sqrt{\Omega_M(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda}.$$

Cosmological N-Body simulations: work well for large scales ($>0.1-10$ Mpc)



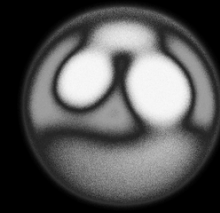
Ingredients

- Cold gravitating components
- Cosmological Constant



Initial Conditions

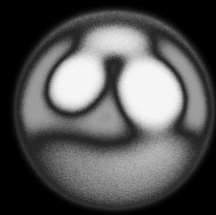
Gaussian initial field
(primordial fluctuation
right after Big Bang)



Physics

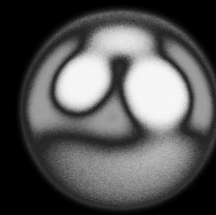
- GR at background level
- gravity

Cosmological N-Body simulations: work well for large scales ($>0.1-10$ Mpc)



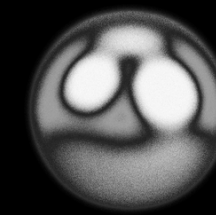
Ingredients

- Cold gravitating components
- Cosmological Constant



Initial Conditions

Gaussian initial field
(primordial fluctuation
right after Big Bang)



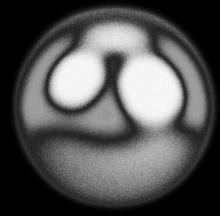
Physics

tions are obtained in a quasi-Lagrangian fashion. For cosmological simulations, gravity is treated in a fully Newtonian framework using periodic boundary conditions. The solution of the general relativity equations (i.e. the Friedman–Lemaître–Robertson–Walker equations with null curvature) determine the expansion (or contraction) of space as a function of cosmic time. Spatial quantities and coordinates are expressed in comoving units, where the mapping between the scale factor a and cosmic time depends on the adopted cosmological parameter values.

Illustris magnetohydrodynamical
cosmological simulations, Pillepich+2017

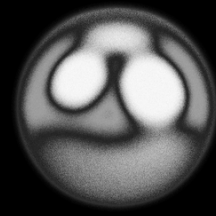
Cosmological hydrodynamical simulations:

most powerful tool to study stellar halos (galaxies, galaxy clusters, etc)



Ingredients

- Cold gravitating components
- Cosmological Constant
- baryons



Initial Conditions

Gaussian initial field
(primordial fluctuation
right after Big Bang)



Physics

- GR at background level
- gravity
- hydrodynamics, star formation and evolutions, feedback (winds/SN/AGNs), blackholes

Cosmological hydrodynamical simulations: Powerful. Yet, challenges remain

computationally
expensive (20–100X
more than DM only)

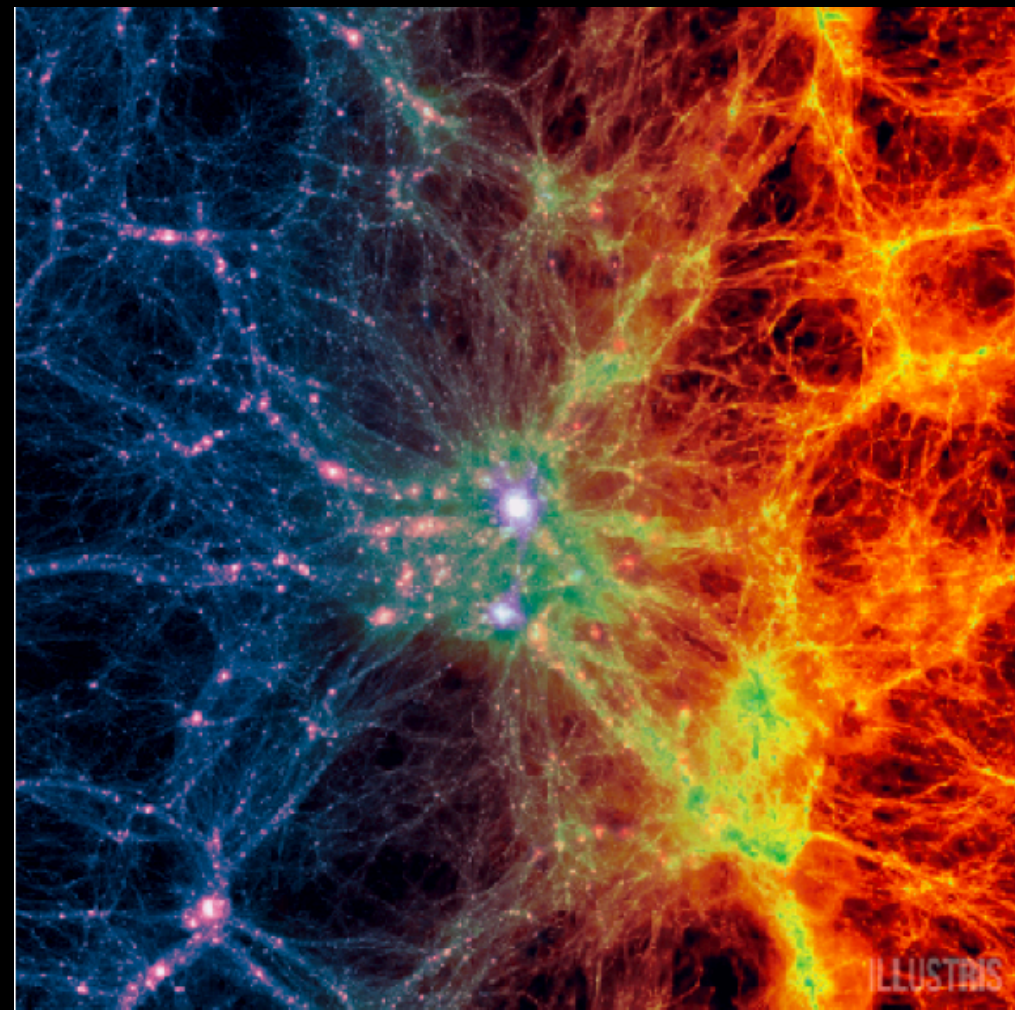
Unresolved physics remain
→ assumptions on star
formation, feedback etc

Cosmological hydrodynamical simulations:

There are two main kinds

Big Box simulations

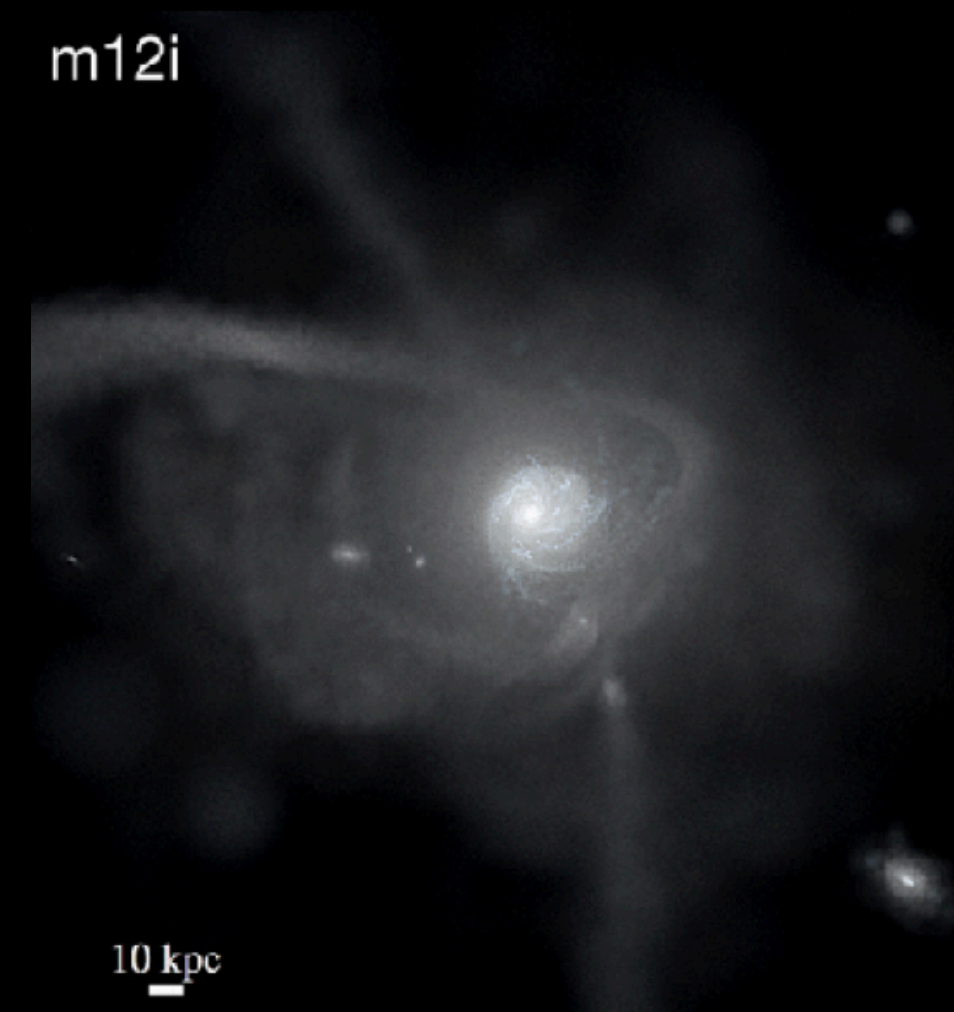
Illustris, EAGLE, Horizon-AGN,...



Zoom-in simulations

FIRE, APOSTLE, NIHAO,...

m12i



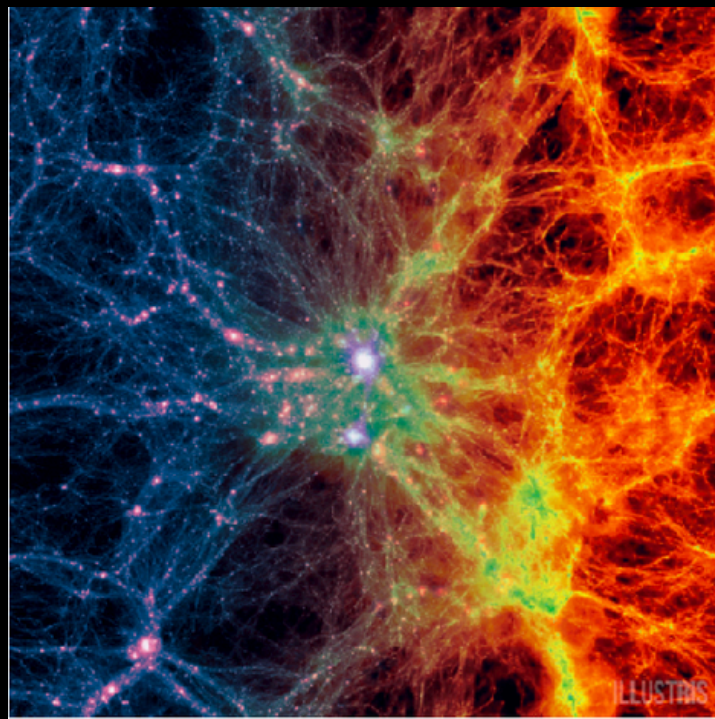
Cosmological hydrodynamical simulations:

There are two main kinds

Big Box simulations

Illustris, EAGLE, Horizon-AGN,...

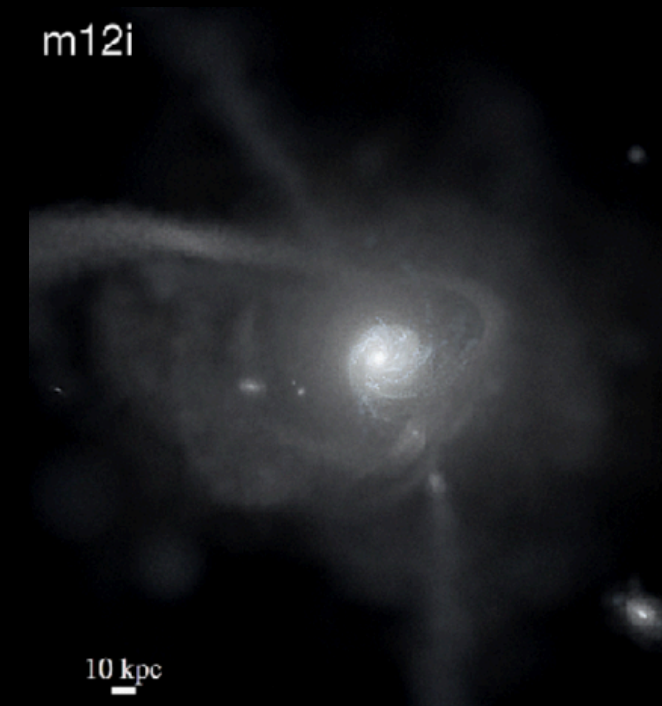
Low resolution but large --> good for large scale structures, statistic samples



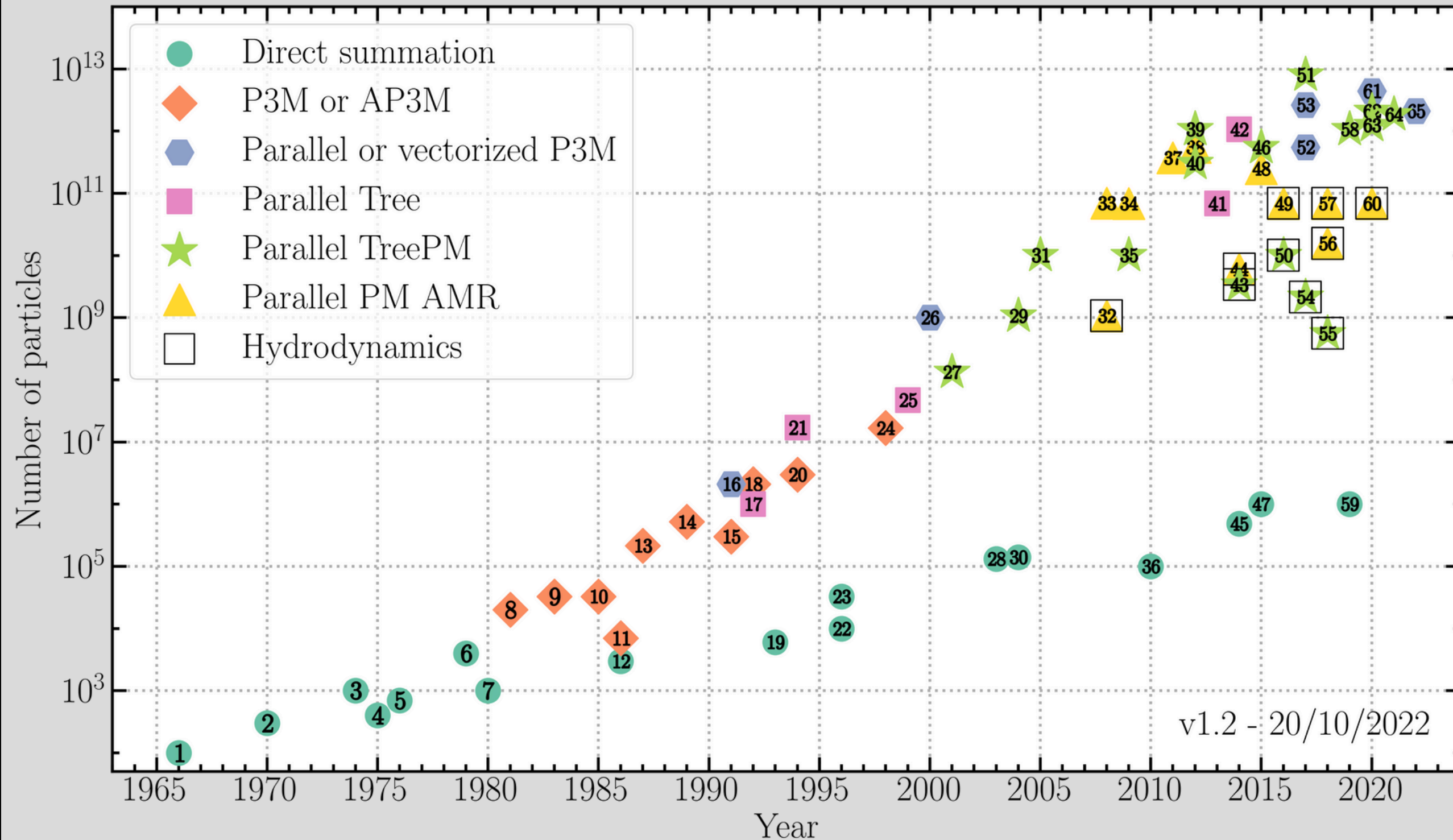
Zoom-in simulations

FIRE, APOSTLE, NIHAO,...

High resolution but small samples --> better tools to study small scales such as giant molecular clouds, star clusters, satellite galaxies

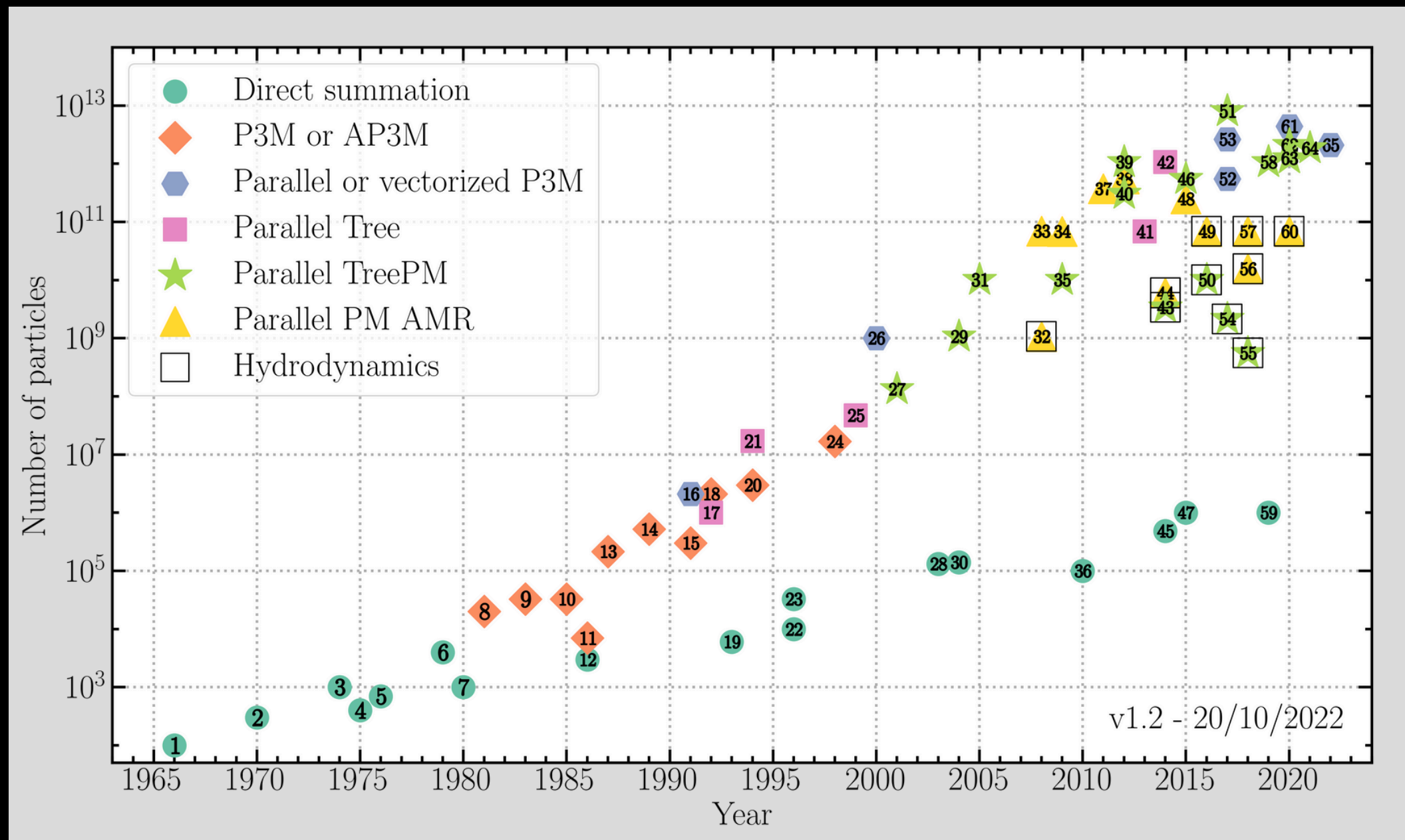


Number of particles in N-body simulations has been increasing exponentially



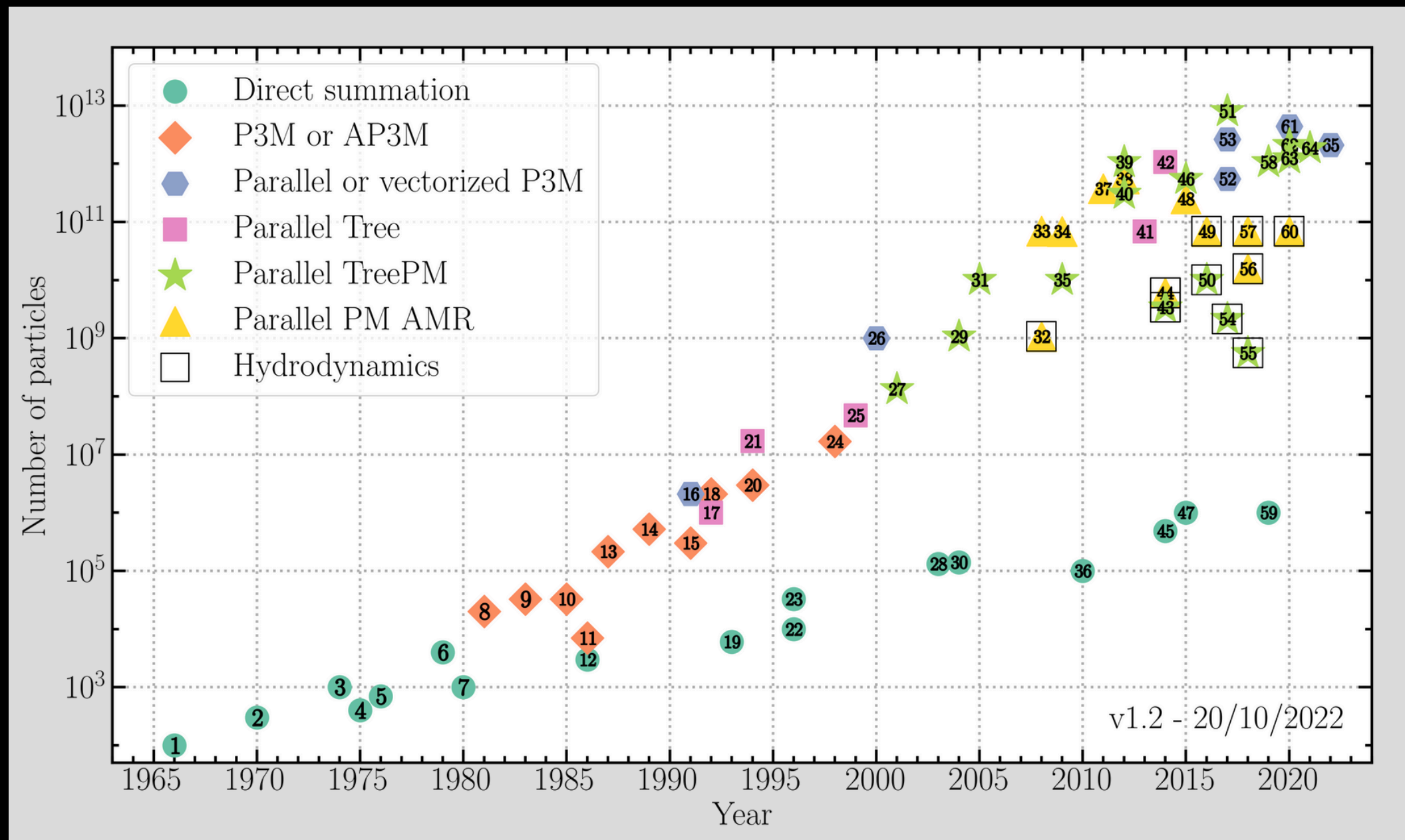
- 31 - Millenium
- 43 - Eagle
- 55 - FIRE-2
- 56 - Illustris-TNG
- 62 - Uchuu

Number of particles in N-body simulations has been increasing exponentially



31 - Millenium : 500 cMpc
 43 - Eagle : 25-100 cMpc
 55 - FIRE-2 : ~25 cMpc
 56 - Illustris-TNG : 50-300 cMpc
 62 - Uchuu : 140 cMpc

Number of particles in N-body simulations has been increasing exponentially



31 - Millenium : 500 cMpc
 43 - Eagle : 25-100 cMpc
 55 - FIRE-2 : ~25 cMpc
 56 - Illustris-TNG : 50-300 cMpc
 62 - Uchuu : 140 cMpc

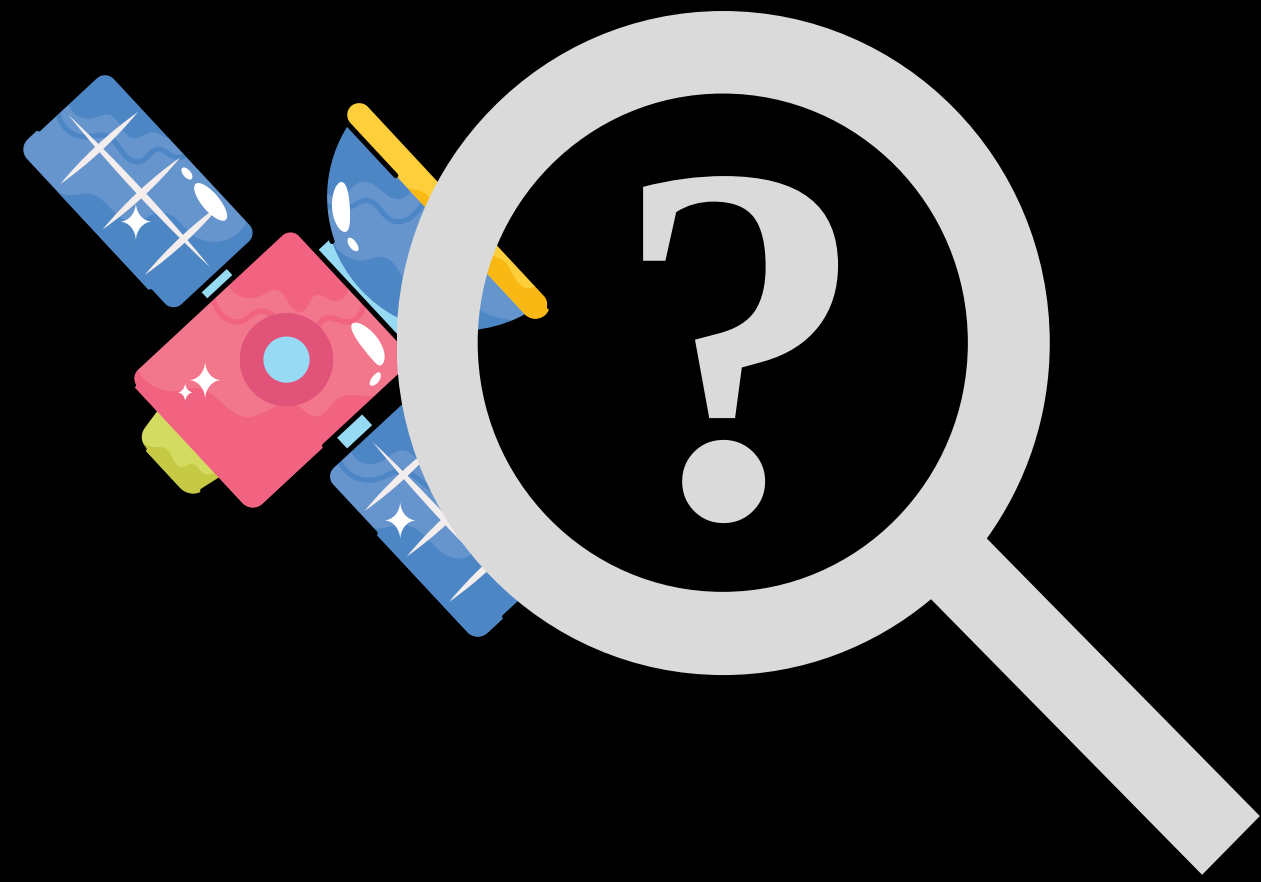
Scales:

galaxy stellar mass: 10^6 - 10^{12} Msun

galaxy size: 1-10 kpc

distance between galaxies: 1 Mpc

Universe size: 15000 Mpc



Missing satellites problem

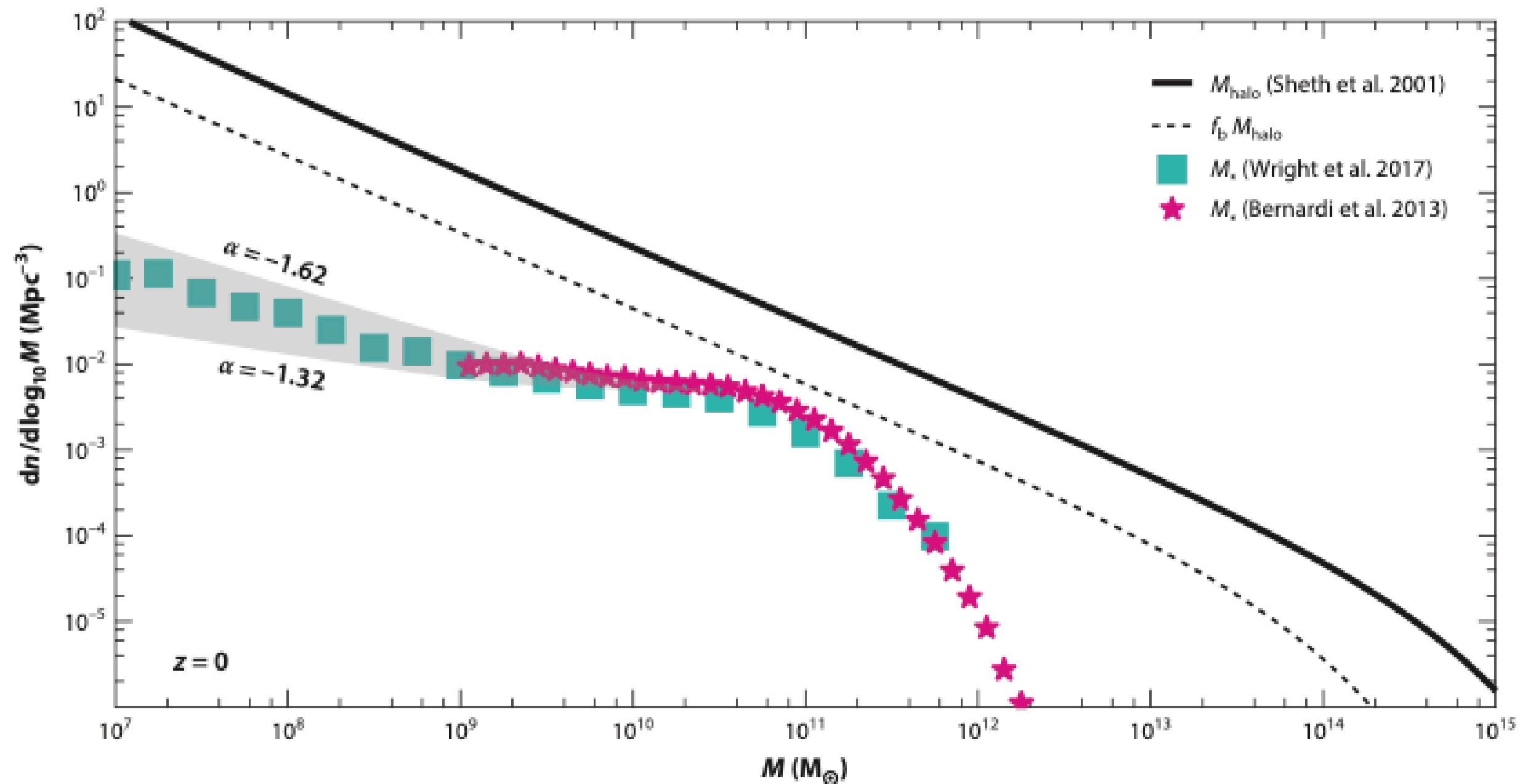
The problem is noticed even at the early dark matter only simulations

Method to relate dark matter halos in the simulations to
observed light from stars and gas (baryons) in galaxies

Abundance matching

Abundance matching

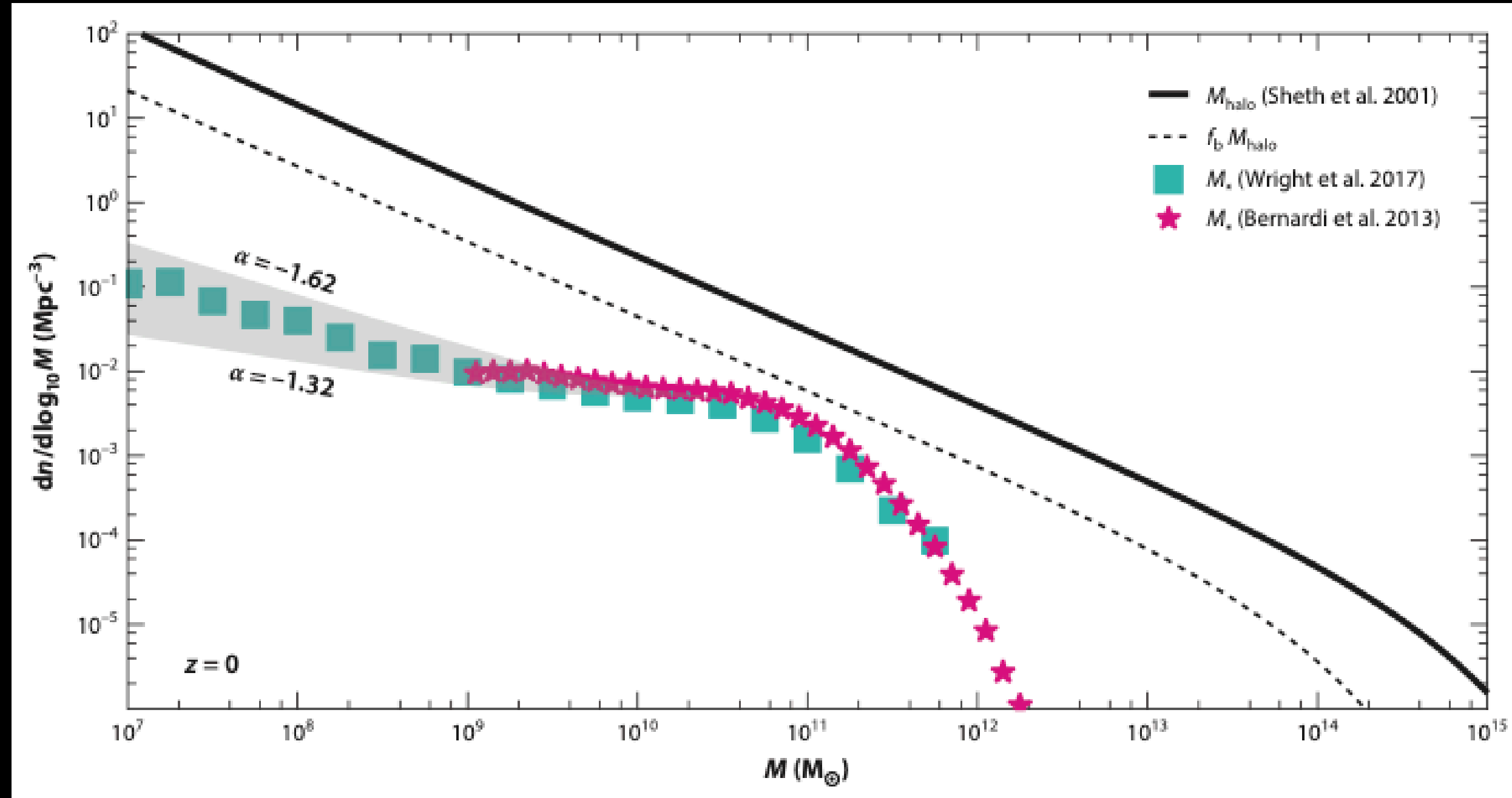
Main assumption:
Galaxies and dark matter halos are related in a one-to-one way; the most massive galaxies live in the most massive dark matter halos



In principle, $M_{\text{halo}} > 10^7 M_{\odot}$ should be large enough to support molecular cooling

Abundance matching

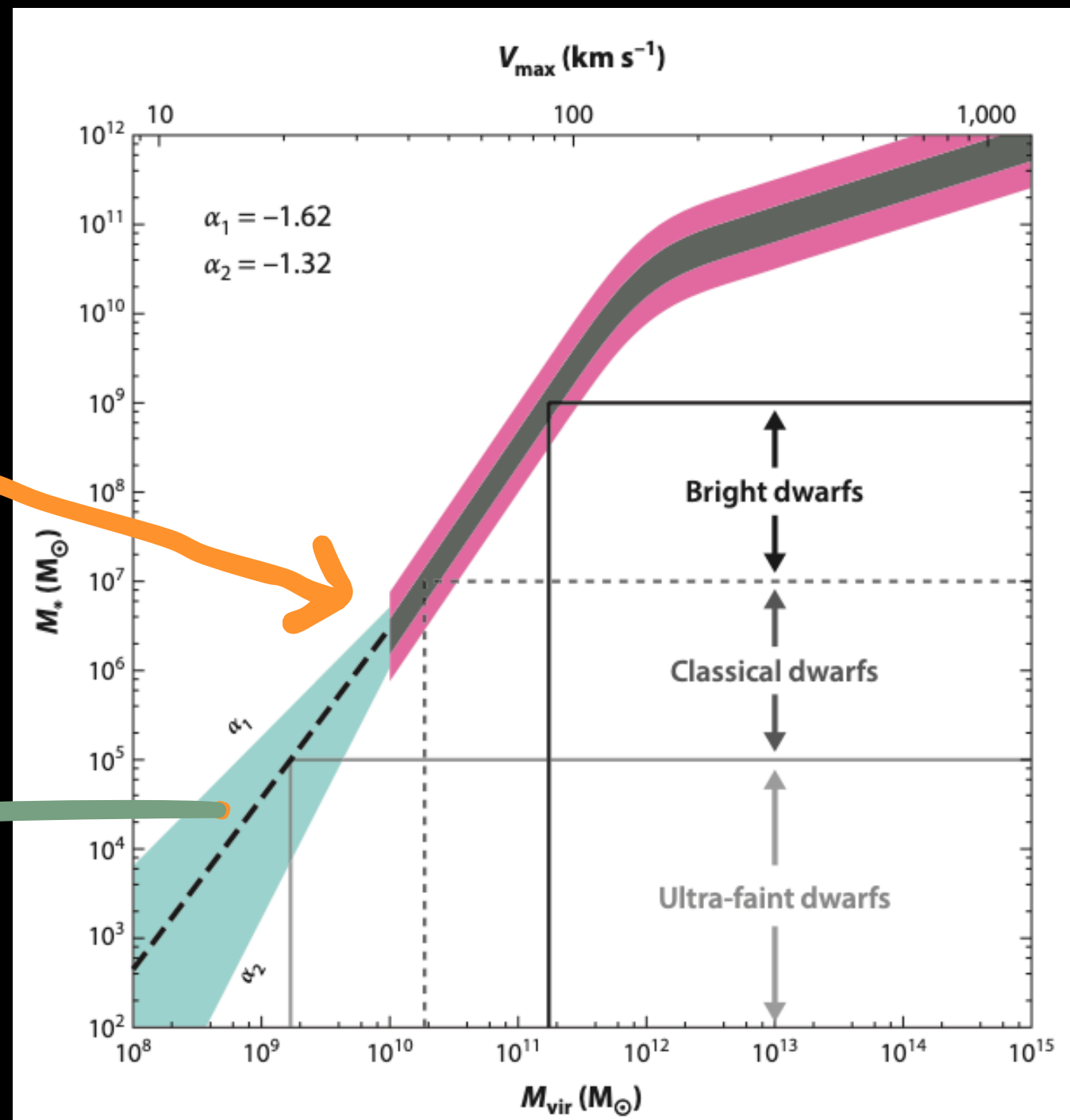
Main assumption:
Galaxies and dark matter halos are related in a one-to-one way; the most massive galaxies live in the most massive dark matter halos



The results of the abundance matching is the relationship between virial mass (\sim halo mass) and stellar mass

limit of observation

Does the unobserved population really follow this trend? Are there that many of them?

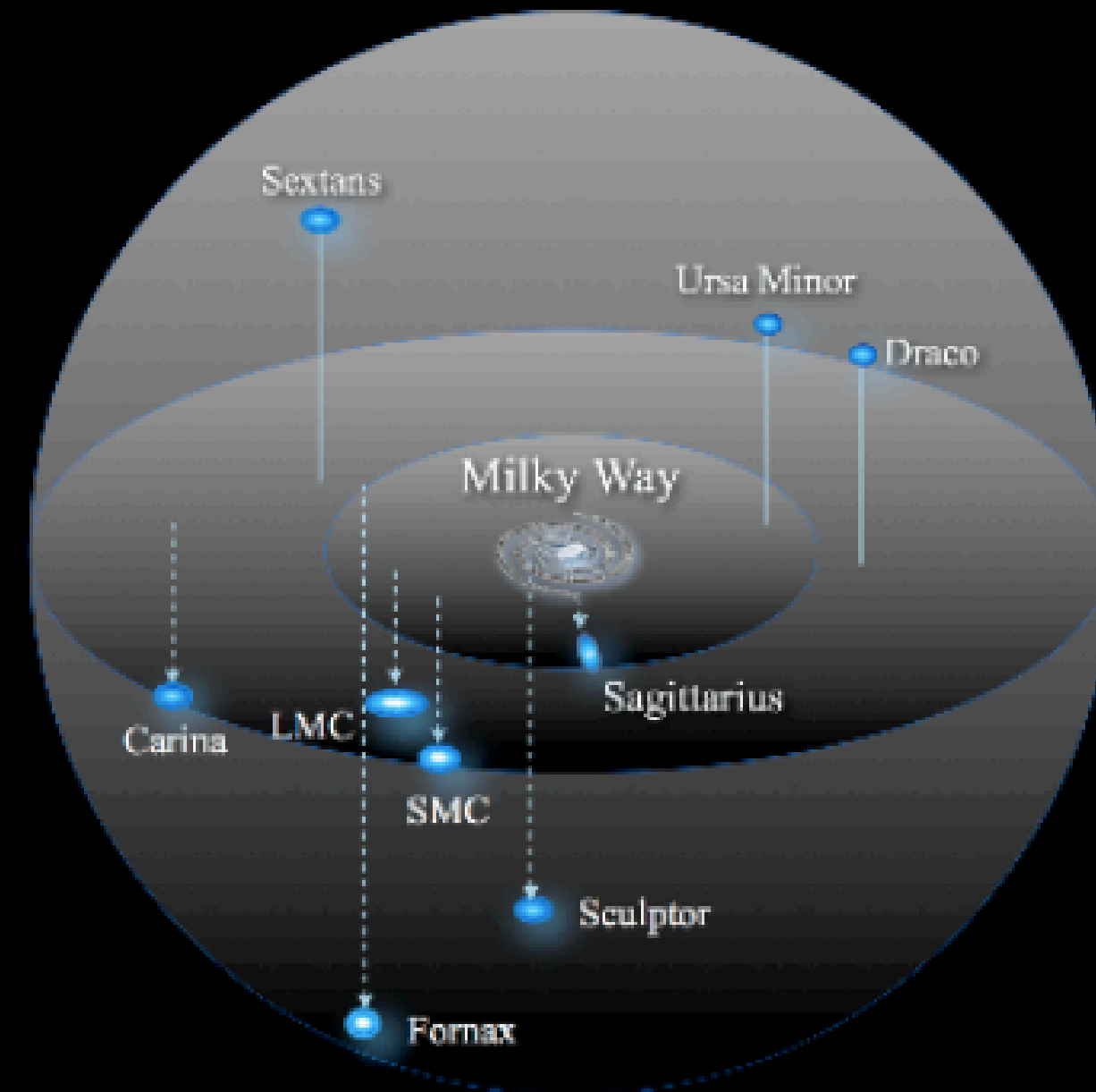


It is unlikely that there are thousands of undiscovered dwarf galaxies

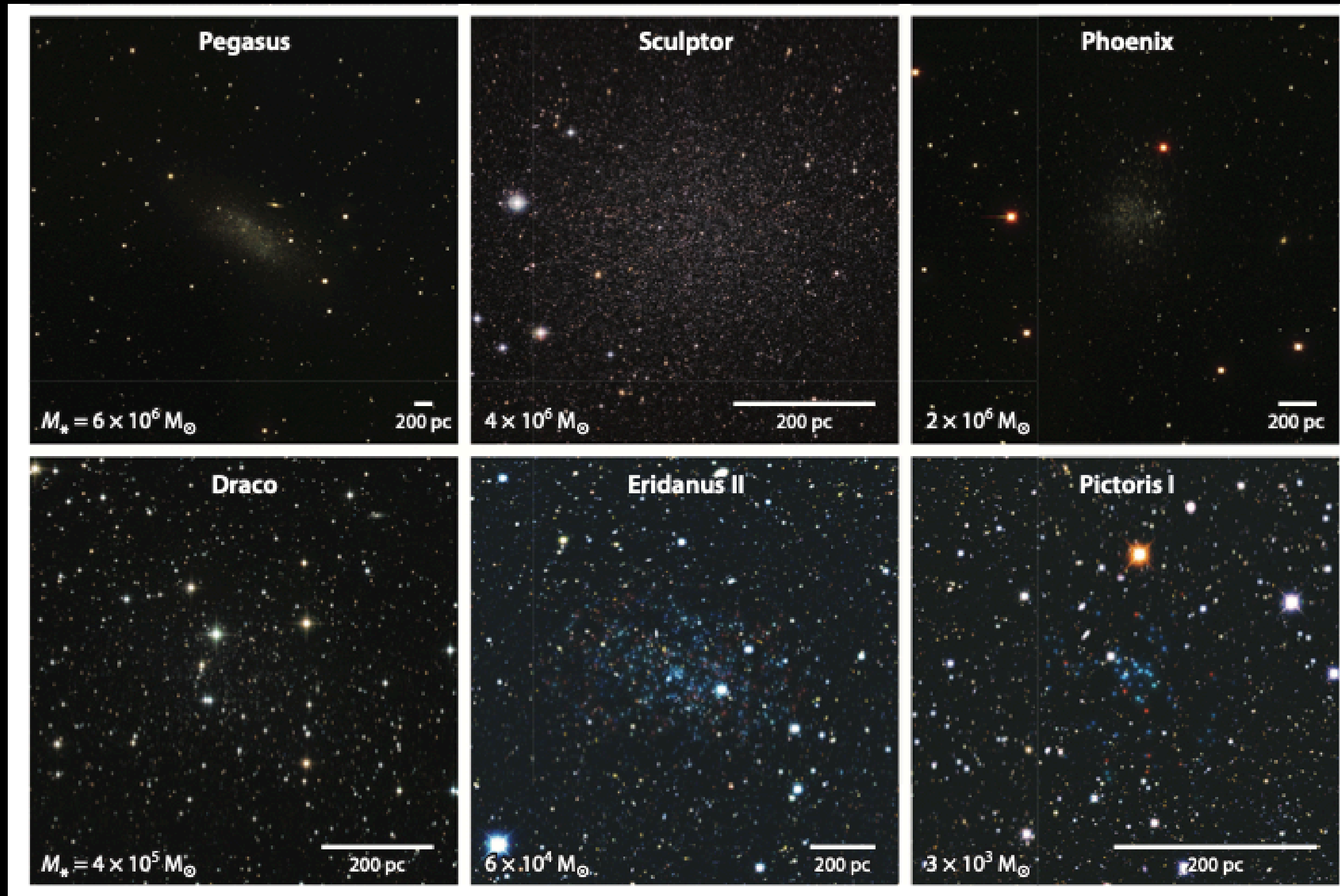
Simulation

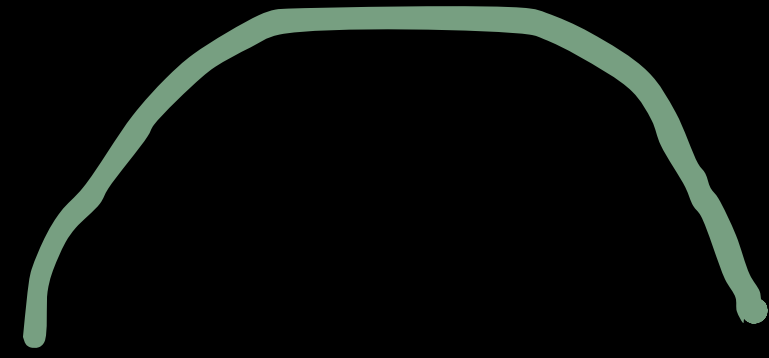
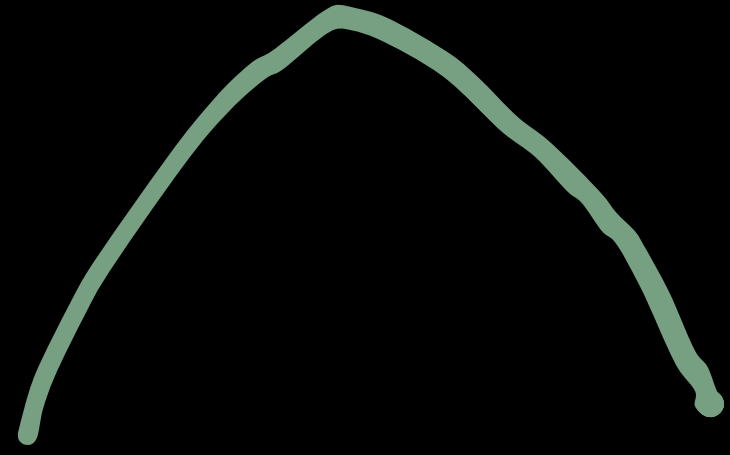


Observation



Not suggesting any solutions, but to point out how difficult to detect dwarf galaxies





Cusp - Core problem

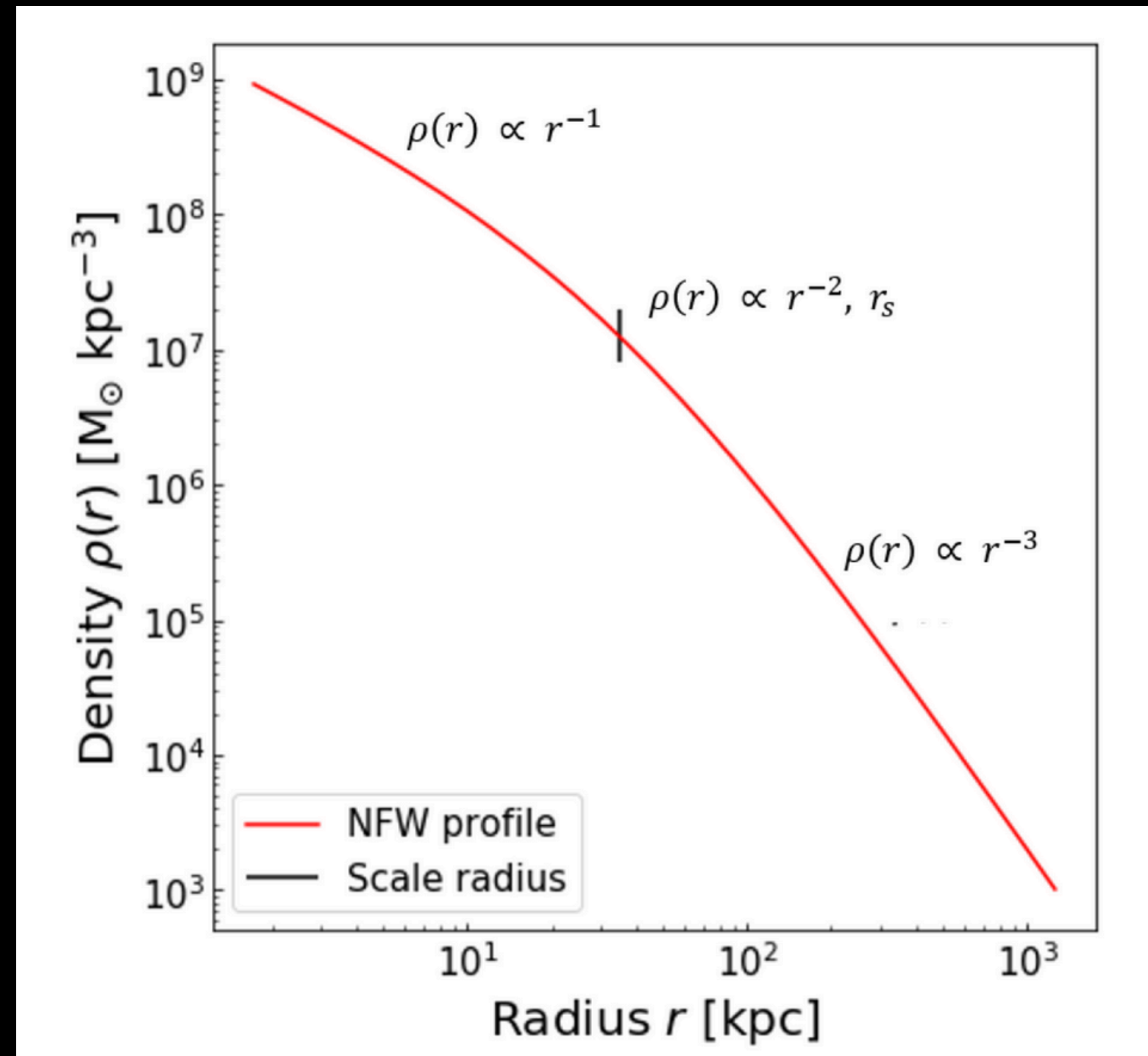
Cold dark matter halos in simulations show the profile that is cuspy in the middle

NFW profile

$$\rho(r) = \frac{4\rho_{-2}}{(r/r_{-2})(1 + r/r_{-2})^2}$$

What happen at large r? What about small r?

Cold dark matter halos in simulations show the profile that is cuspy in the middle



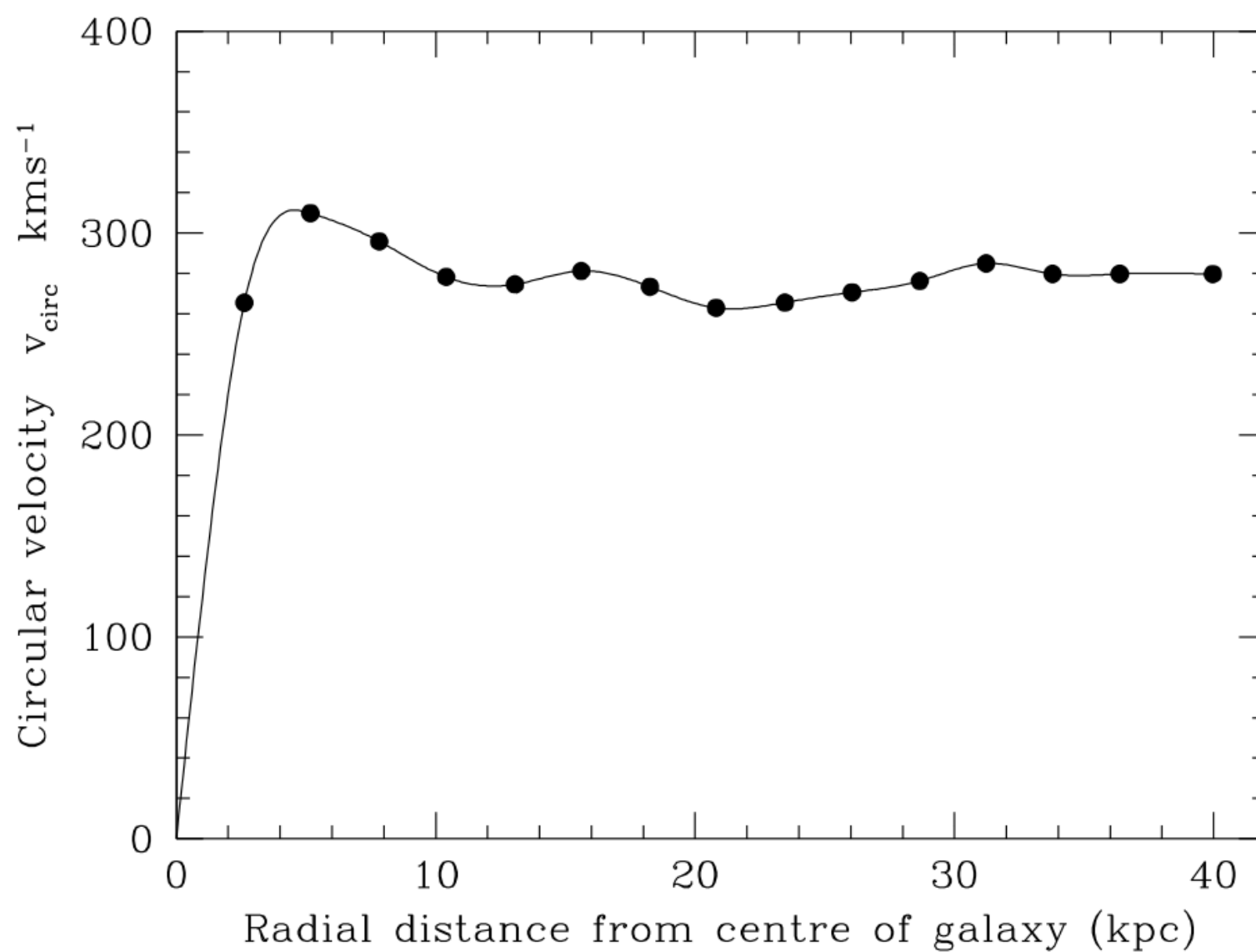
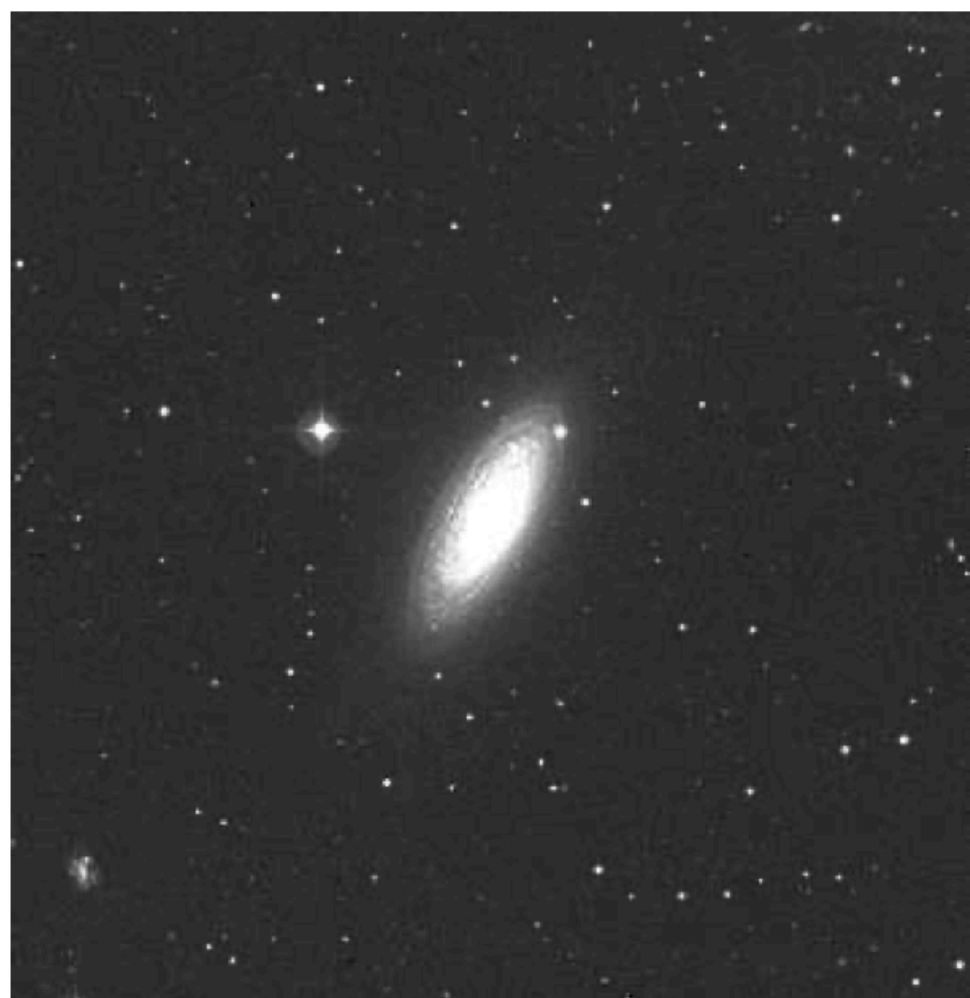
NFW profile

$$\rho(r) = \frac{4\rho_{-2}}{(r/r_{-2})(1 + r/r_{-2})^2}$$

Observationally, another way to relate dark matter to observable is via rotation curve (in addition to abundance matching)

$$\frac{v_{circ}^2}{R} = \frac{GM(R)}{R^2}$$

**First rotation curves were measured in 1970s.
Soon we found that disc galaxies have flat
rotation curves.**

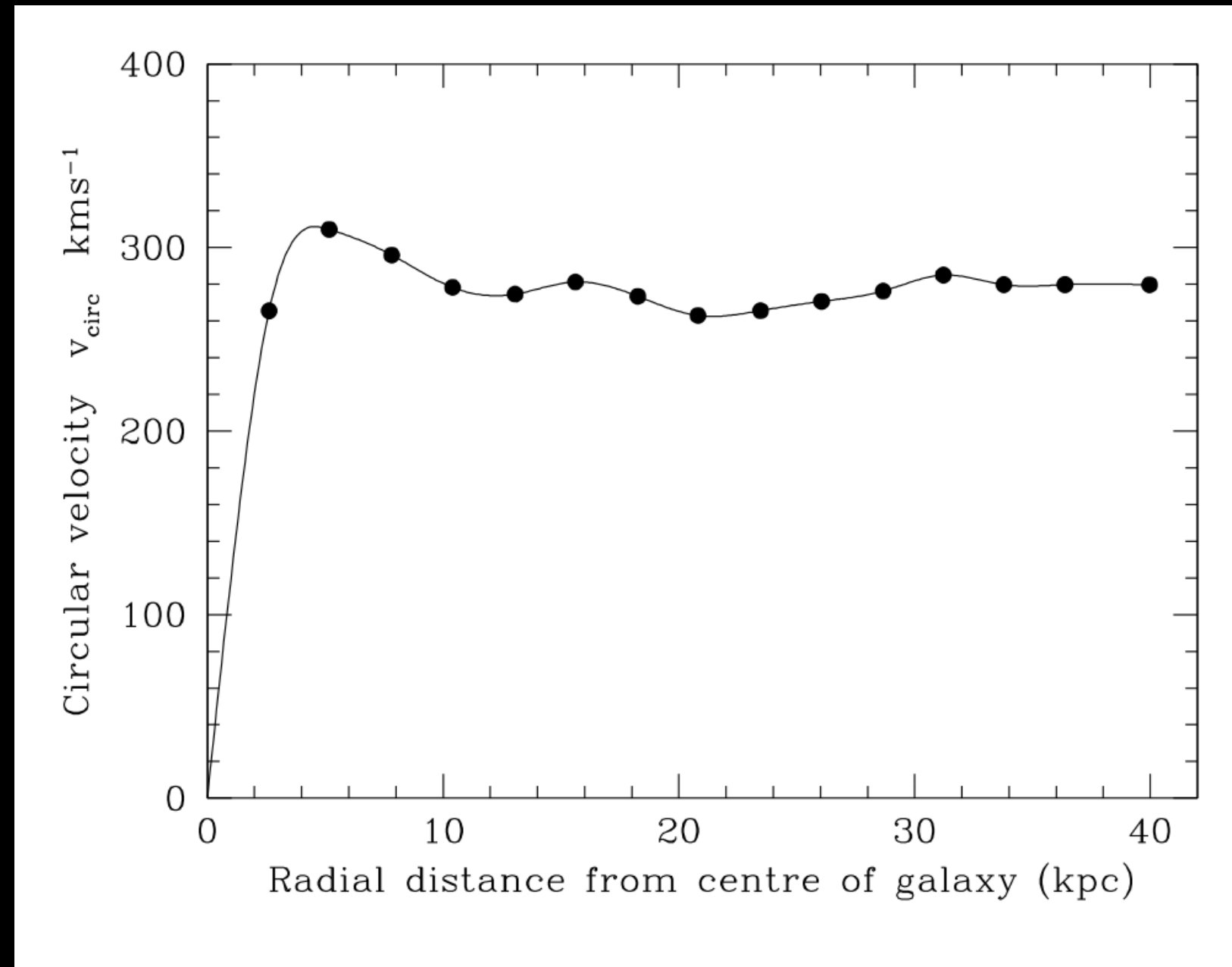


What does flat rotation curve mean? Is it consistent with NFW profile?

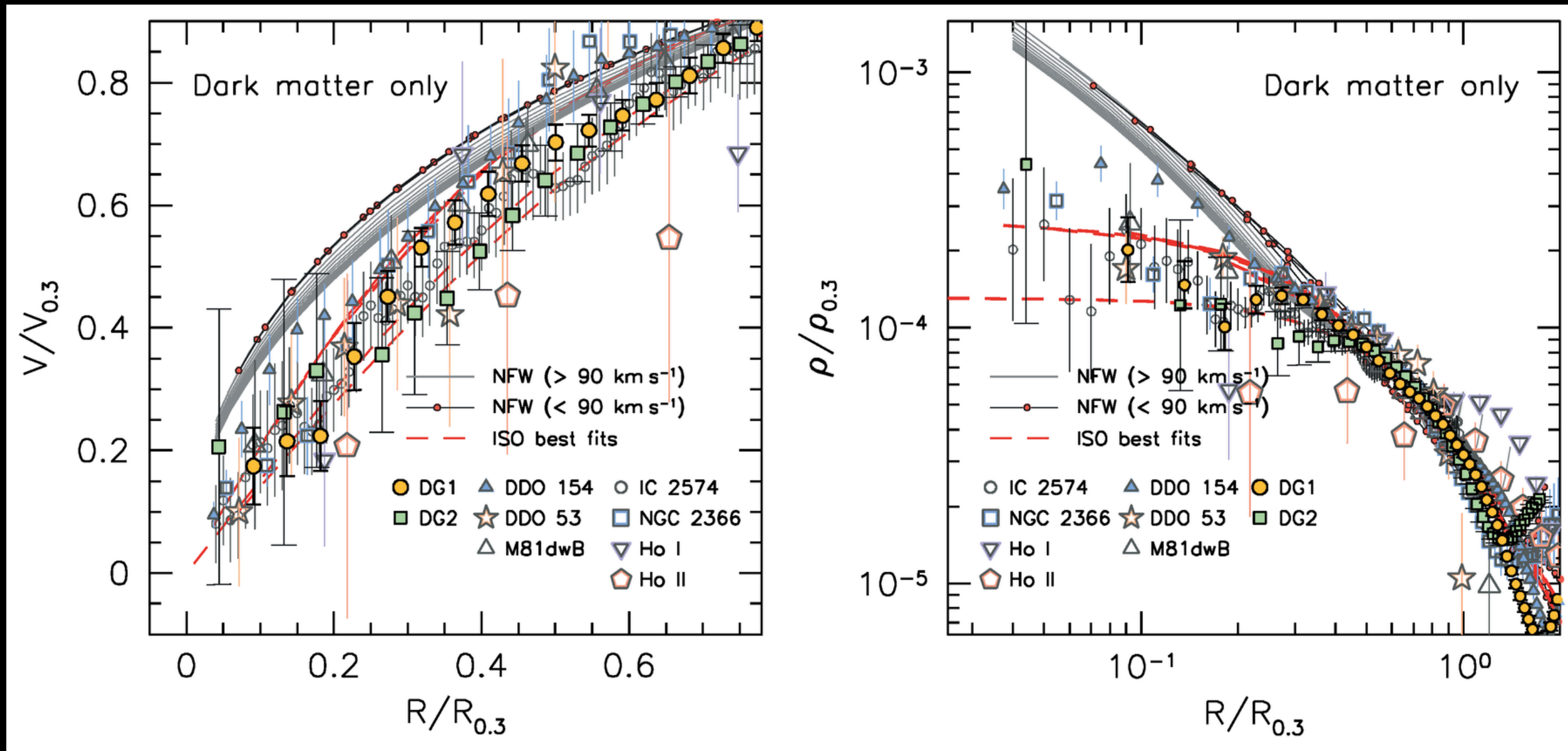
$$\frac{v_{circ}^2}{R} = \frac{GM(R)}{R^2}$$

NFW profile

$$\rho(r) = \frac{4\rho_{-2}}{(r/r_{-2})(1 + r/r_{-2})^2}$$

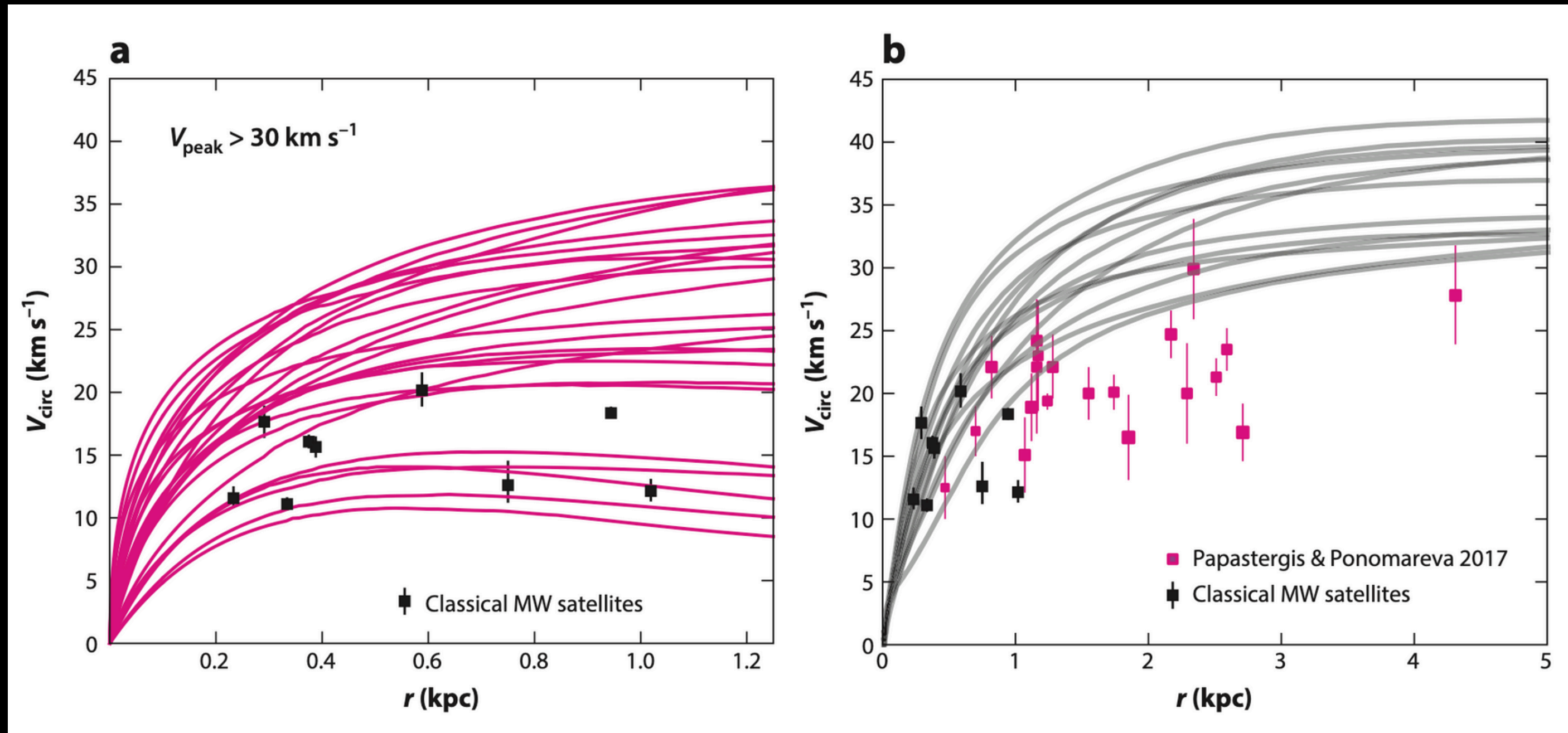


When we measure the rotation curves in the inner core of dwarf galaxies we found that they all have flat density profile at the core



Too big too fail problem

When we measure the rotation curves in the inner core of dwarf galaxies we found that they all have flat density profile at the core

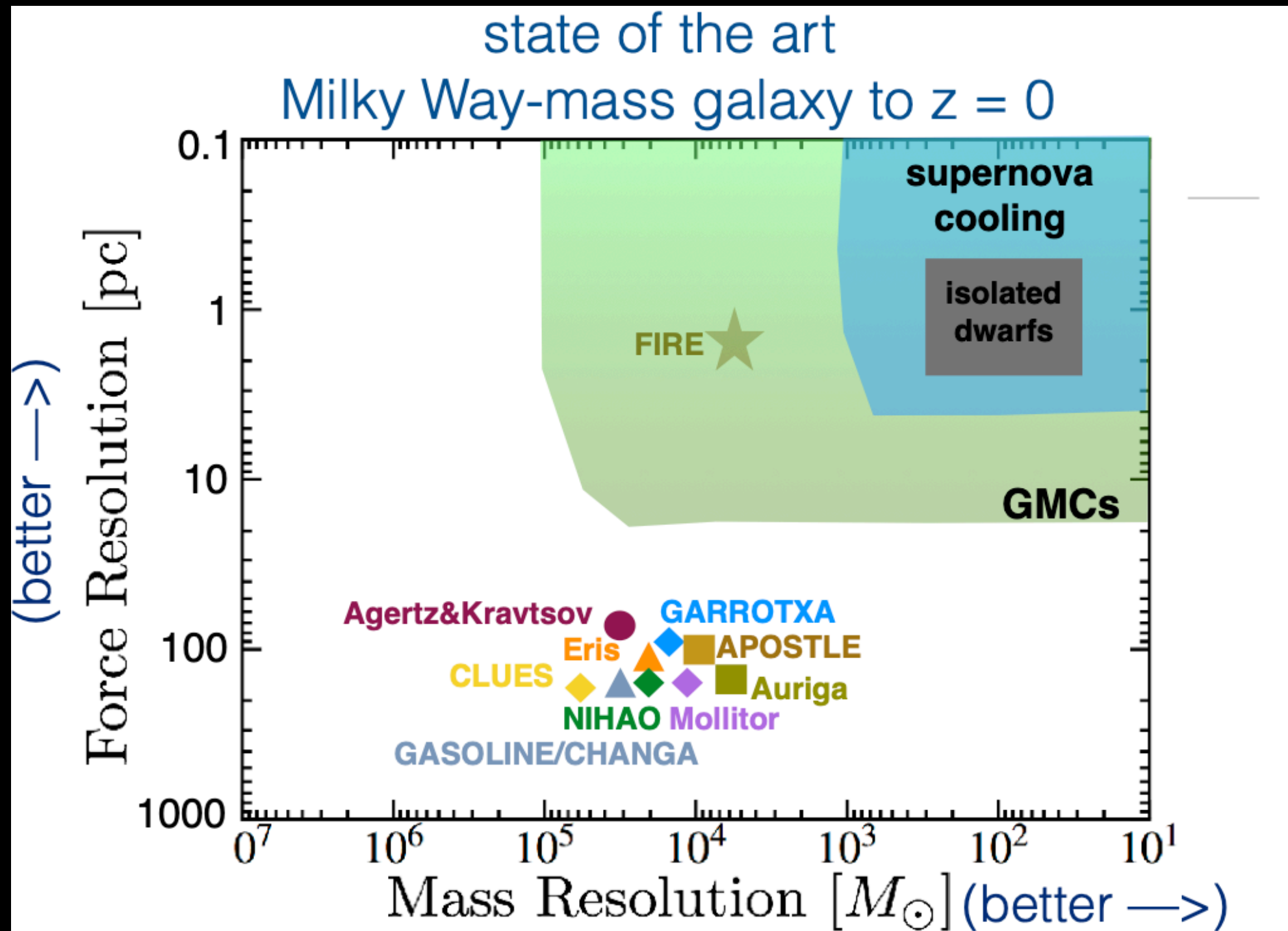


Your turn to look for solutions

Lambda-CDM

Simulations

Observation



Conclusion:

galaxy stellar mass: 10^6 - 10^{12} M_{sun}

galaxy size: 1-10 kpc

distance between galaxies: 1 Mpc

Universe size: 15000 Mpc

Wetzel+2016 RECONCILING DWARF GALAXIES WITH Λ CDM COSMOLOGY: SIMULATING A REALISTIC POPULATION OF SATELLITES AROUND A MILKY WAY-MASS GALAXY

Kim+2016 There is No Missing Satellites Problem

Slide adapted from <https://www2.mpia-hd.mpg.de/homes/stellarhalos2018-loc/sh2018/slides/02.07.Wetzel.pdf>