

# Méthode de comparaison de performances de fiabilité de différents matériels roulants

## Methodology to compare different rolling stock reliability performances

MILLIOT Frédéric  
*Senior RAM Expert*

ASLTOMSAINT OUEN sur SEINE  
[frederic.milliot@alstomgroup.com](mailto:frederic.milliot@alstomgroup.com)

### 1 **RÉSUMÉ/SUMMARY**

2 This paper presents a method to compare different rolling stocks performances eradicating the bias introduced by different  
3 mission profiles (mileage and speed). Once the scope of study is defined (can be at train level, at subsystem level or lower), the  
4 starting point is to perform Reliability Growth models for each product, on a defined set of field data. Alstom uses the Crow-  
5 AMSAA model which has a good ability to fit data, especially for the end of the observation. Then, it is possible to plot  
6 Reliability Growth Curves for each product by using a single and referenced mileage profile defined by the study. It is also  
7 necessary to suppress the speed influence on the failure intensities (generally measured in  $\text{km}^{-1}$ ); to do that a correction is done  
8 “as if” all the products had the same referenced commercial speed. Finally, this comparison is the introduction to a qualitative  
9 analysis to determine the best practices and best solutions in the reliability perspective.

10 Cette publication présente une méthode de comparaison de performances de fiabilité de différents matériels roulants qui  
11 supprime le biais introduit par des profils de mission kilométriques et de vitesses qui sont nécessairement différents. Une fois  
12 le périmètre de l'étude établi, son point de départ est de réaliser des modèles de croissance de fiabilité sur des données de terrain  
13 pour chacun des produits sélectionnés. Alstom recommande le modèle de Crow-AMSAA pour sa capacité à ajuster les données,  
14 spécialement les derniers points d'observation. Dès lors, il devient possible de tracer les courbes de croissance de fiabilité sur  
15 un profil de mission kilométrique unique dit de référence. De manière analogue, on doit corriger l'influence des vitesses  
16 moyennes qui influent sur l'intensité de fiabilité (mesurée en  $\text{km}^{-1}$ ); la comparaison se déroule « comme si » les flottes de trains  
17 avaient la même vitesse moyenne. Au final, cette comparaison vise à lancer une analyse de causes qualitative devant déterminer  
18 les bonnes pratiques et les solutions pour garantir la fiabilité.

### 19 **MOTS-CLEFS/KEY WORDS —**

20 Comparison, Reliability Growth, mission profile, Crow-AMSAA, and lessons learnt.

### 21 **I. INTRODUCTION**

22 In the Railway industry, reliability is a key performance and become more and more challenging. The customer targets  
23 become more and more stringent and intermediate objectives can also be defined. The customers want the best reliability as  
24 soon as possible after the manufacturer's delivery. In this context, the rolling stock is one of the most critical systems in terms  
25 of reliability. The reason is mainly due to a high complexity and the integration of multiple functions. The financial risk for a  
26 company like Alstom is important. Indeed, the consequences of service perturbation are huge: potential penalties, fees, the cost  
27 of spare parts, maintenance workload, cash payment milestone or other contractual clauses.

28 So, the management of reliability performance is critical. One way to manage this risk is to predict the performance and, by  
29 anticipation, take actions to optimize or improve the reliability. Practically there are 2 possible ways to perform this prediction

- 30 • a theoretical one which is a combination of figures from supplier's studies which is not addressed in this paper
- 31 • another one use Return of EXperience performances from previous projects.

32 Ideally, both approaches are combined since the tender stage of the project. The first approach provides a steady state  
33 prediction.

34 The second one could provide better confidence in the result but introduce bias due to the specific conditions of the projects.  
35 So at the company level, it is necessary to be able to capitalize this REX and get the best estimations from that. One use case  
36 is to use the REX to predict performance for a new projects since the tender stage to estimate the risk of non-compliance.  
37 Another use case is to compare on field project performances and identify quantitatively which one is the best/worst product in  
38 a family; this is the topic of this article. Once this identification is done, the good and bad practices as well as the good and the  
39 bad solutions can bring lesson learnt to improve the future products.

40 The main challenge faced to perform this comparison is that every product is slightly different from each other, but, in  
41 addition, the customer mission profiles can also vary (speeds, mileage, power on time, time in service,...), as well as the size of  
42 the fleet (can be between 10 to 50 trains), the commercial service introduction planning of the train are different, the observed  
43 fleet mileages are different (between 3 and 15 million kilometers) and the various climates must be considered. So many different  
44 factors can influence the comparison.

45 The goal of this method is to eradicate at least the bias introduced by the mission profile, that is to say the difference of  
46 mileage run by the fleets and the average commercial speeds. The main idea is to use the Reliability Growth Models and the  
47 referenced conditions of mileage and speed to simulate performances as if all products were operated in the same condition. In  
48 this way, the comparison is becoming possible and correct. This paper presents a methodology breakdown in 5 steps.

## 49 II. REVUE DE LITERATURE

50 [CROW] AMSAA Technical report n° 138 Reliability Analysis for complex, repairable systems, Larry Crow 75

51 [IEC] IEC 61710:2013 Power law model – Goodness-of-fit tests and estimation methods

52 [DUANE] "Learning Curve Approach To Reliability Monitoring," Duane, J.T. 64

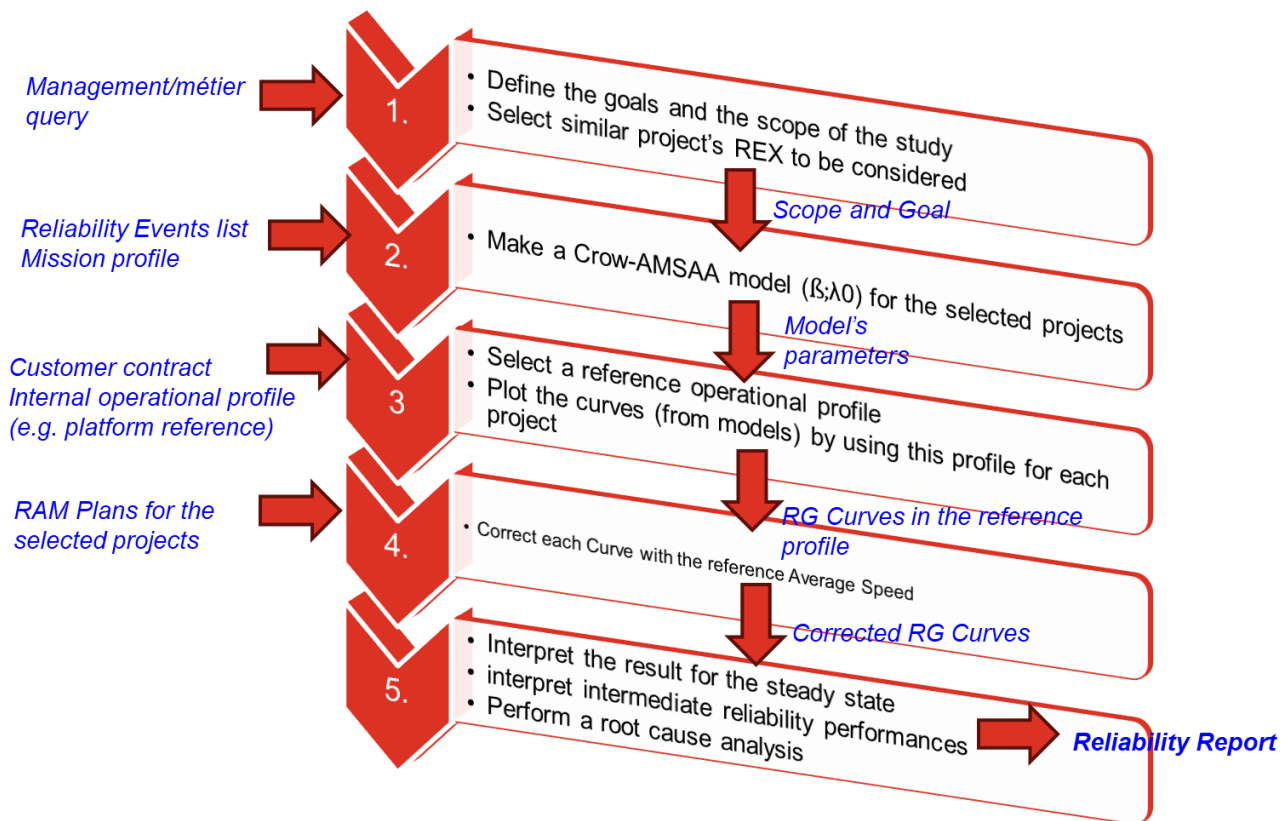
53 [TAN] MATHEMATICAL ASPECTS OF RELIABILITY GROWTH ANALYSIS, TANANKO, 2019

54

## 55 III. METHODOLOGY OVERVIEW

56 The proposed methodology is structured into five distinct steps, as illustrated in Figure 1:

57



58

59

Fig. 1. Methodology Diagram

60 IV. DEFINE THE SCOPE AND THE GOAL OF THE ANALYSIS

61 The initial step involves defining the objective of the analysis. This goal may originate from various sources such as a  
62 management directive, a tender requirement, or internally from pure Reliability, Availability or Maintenance concerns.

63 Possible objectives include: assessing whether the previous generation of metros performs better than the new one,  
64 determining the benchmark product within a certain range to offer customers, or demonstrating that a product meets or exceeds  
65 a benchmark standard. Once the objective is established, we identify the relevant projects for methodological development. This  
66 involves collecting raw data and key mission profile characteristics from the warranty phase, during which each incident's service  
67 impact is evaluated by both the customer and the manufacturer. The current method is not modifying the content of those data,  
68 the only action is to group all Service Affecting Failure (SAF) in a global one. Then we can plot the reliability in term failure  
69 intensity vs observed mileage.

70 In the railway industry the Mean Distance Between Failure or the Failure intensity are used to measure the reliability. As  
71 defined in [IEC] like:

72 
$$FI(t) = \frac{d(E(N(t)))}{dt} \quad (1)$$

73 with  $N(t)$  the number of events and  $E(N(t))$  the mean value of events.

74 We cannot use directly this formula, we have to transform it into a mileage base:

75 
$$FI(km) = \frac{d(E(N(km)))}{dkm} \quad (2)$$

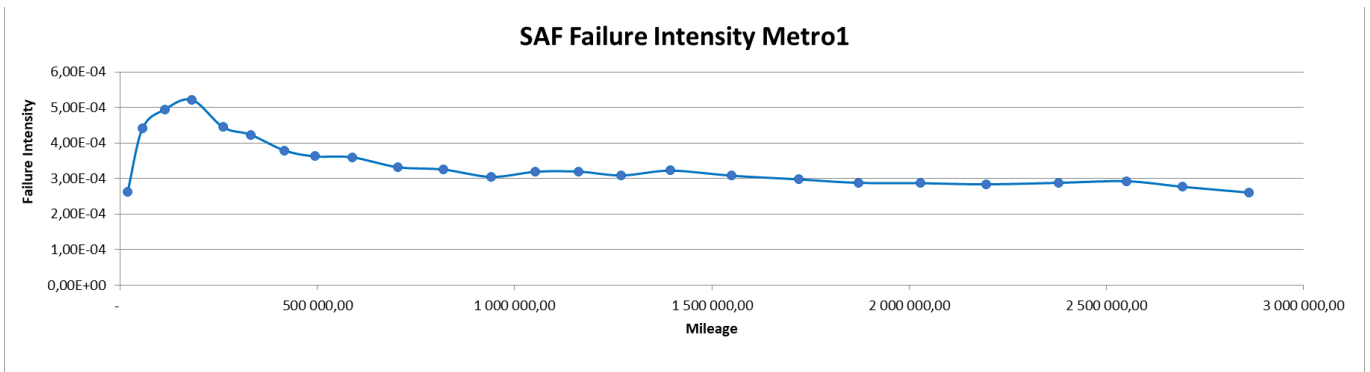
76 Thus the estimator is:

77 
$$FI_{estimator}(km) = N(km)/km \quad (3)$$

78 This is what is usually measured in the projects.

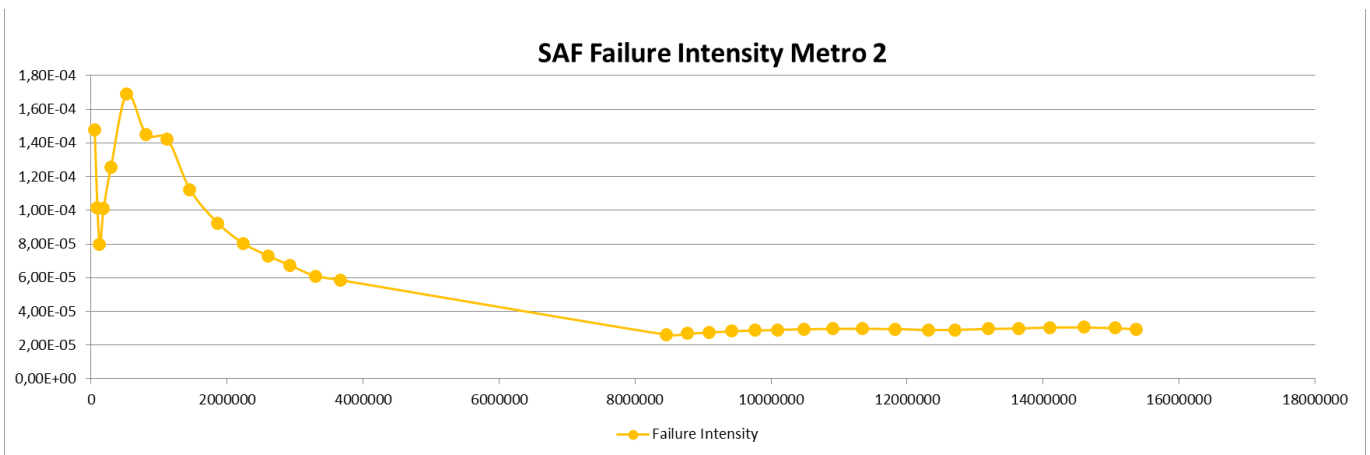
79 For illustration, consider a study aimed at comparing two metro fleets.

80 Metro 1 comprises a fleet of 23 trains observed over a 3 million km cumulated distance. By plotting the Service Affecting  
81 Failure intensity vs mileage it comes fig 2:



82  
83 Fig. 2. Measured SAF Failure Intensity for Metro 1

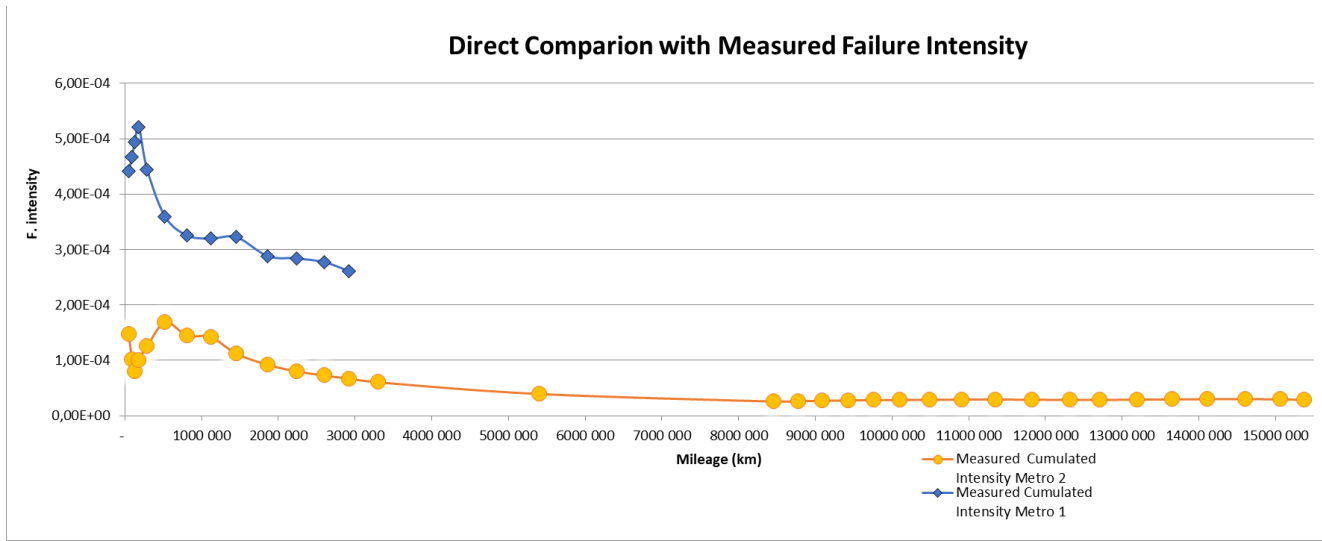
84 Metro 2 consists of a fleet of 50 trains, observed over 16 million km cumulated distance see fig 3:



85  
86 Fig. 3. Measured SAF Failure Intensity for Metro 2

87 Reliability Growth (RG) curves are highly useful for evaluating reliability over time, addressing questions such as: 'Is the  
 88 product reaching its optimal performance? What are its intermediate performance milestones (e.g., after X months or Y  
 89 kilometers)? What is its initial reliability?' The mean value may not accurately represent the best performance achievable,  
 90 highlighting the importance of RG curves.

91 For the objective of this analysis—comparing Metro 1 and 2—we attempt a direct comparison by overlaying both curves on  
 92 the same graph, aligning them along the same mileage on the X-axis, as shown in: Fig 4:



93 Fig. 4. Direct Performance Comparison with measured Failure Intensities

94  
 95  
 96 Initially, it seems that Metro 2 is significantly more reliable than Metro 1, with Metro 1's failure intensity reaching only 26%  
 97 of that of Metro 2. However, this quick assessment warrants scrutiny. The observation periods differ significantly: Metro 1's data  
 98 is capped at 3 million kilometers (marking the end of its contractual warranty period), compared to 16 million kilometers for  
 99 Metro 2. This discrepancy raises questions: How would Metro 1 perform over an observation period equivalent to Metro 2's?  
 100 Has Metro 1 achieved its optimal performance? Furthermore, the quantity of observations differs between the two fleets, resulting  
 101 in lower confidence in the reliability assessment for Metro 1 compared to Metro 2. Such a 'direct comparison' approach, while  
 102 once considered state-of-the-art, is precisely what the methodology introduced in this article aims to refine.

103 .

104 V. RELIABILITY GROWTH MODELLING

105 The subsequent step in the methodology involves calculating a Reliability Growth (RG) model for each product, offering  
 106 several advantages. Firstly, the model affords a 50% confidence level for any given distance. Secondly, it effectively filters the  
 107 randomness of the observations. Actually, the number of observed events  $N(t)$  can be considered as a random variable with a  
 108 given spread. RG models are able to predict the average value of  $N(t)$ .

109 There are two main models:

- 110 • Duane described in [DUANE]
- 111 • Crow-AMSAA described in [CROW]

112 The difference between those and the assumptions are detailed in [TAN].

113 In a few words and put in the Railway scope of application Duane model postulates that:

114 
$$\ln(N/Cumulated\ km) = \ln(\lambda) - \alpha * \ln(Cumulated\ km) \quad (4)$$

- 115 •  $\alpha$  is the shape parameter
- 116 •  $\lambda$  is the scale parameter

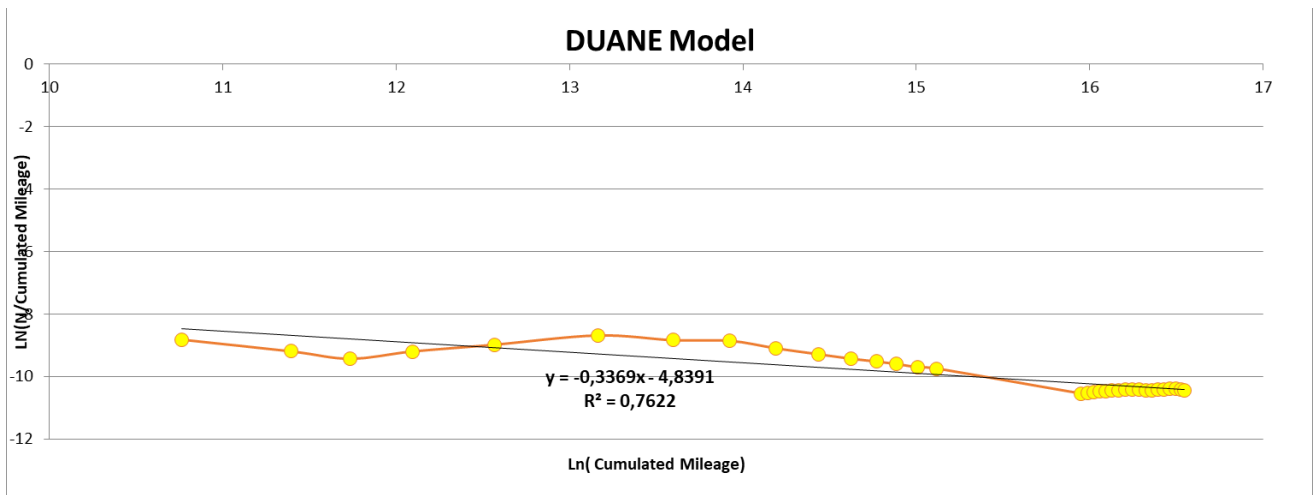


Fig. 5. Duane Parameters estimation

By plotting  $\ln(N/Cumulated\ km)$  on y axle and  $\ln(Cumulated\ km)$  on x axle the parameter's estimation is straightforward.

$$\alpha = -Slope \quad (5)$$

$$\lambda = Exp(Y\ intercept\ for\ x = 1) \quad (6)$$

This can be done with special Reliability Tools or with a spreadsheet with a linear regression. The modelling error can be evaluate with the correlation factor  $R^2$  taken from this linear regression.

Dr. Larry Crow converted the Duane model into a stochastic model using a Weibull distribution as failure intensity function [CROW].

$$Instantaneous\ Failure\ Intensity_{Fleet}(km) = \lambda_0 * \beta * (km)^{\beta-1} \quad (7)$$

- $\beta$  is the shape parameter
- $\lambda_0$  is the scale parameter

in this model the Total Number of events is no more deterministic (as in Duane) and is a random variable.

The model parameters ( $\beta, \lambda_0$ ) are rendered independent of the original mileage, enabling the derivation of an analytical formula for failure intensity (1) from [IEC]

$$Cumulated\ Failure\ Intensity_{Fleet}(Cumulated\ km) = \lambda_0 * (Cumulated\ km)^{\beta-1} \quad (8)$$

The parameters estimation uses the Maximum Likelihood which improve the fitting capabilities compare to the Duane estimation. In this case the calculation is more sophisticated. The algorithm is provided in [IEC] time data for group of relevant failures. Each month, one counts the relevant events for the current month. In addition the actual mileage run by the fleet is collected. This can be done with special Reliability Tools or with a spreadsheet with optimisation capabilities.

This methodology advocates for the use of the Crow-AMSAA model. With the type of data we analyze, it has been observed that this model possesses a superior capability to accurately fit data towards the end of the observation period compared to the Duane model. In figure 6 we present an example of fitting capabilities comparing Duane and Crow-AMSAA for the same set of data. We calculate the errors at each km:

$$Error(km) = \left| \frac{Ncumulated(km)}{km} - Model(km) \right| \quad (9)$$

The Duane model, due to its estimation technique, generates an average prediction that considers the entire history of the process. Given that reliability experience (REX) curves may exhibit irregularities at the start — attributable to gradual train deliveries and the establishment of the customer's operations — the Duane model can introduce discrepancies. The end of the observation is the most important for the manufacturer because it represents the optimal performances of the product for which the customer set a target. With the Duane model the weight of the beginning and the end of the observation are the same, which leads to pessimistic results, most of the time.

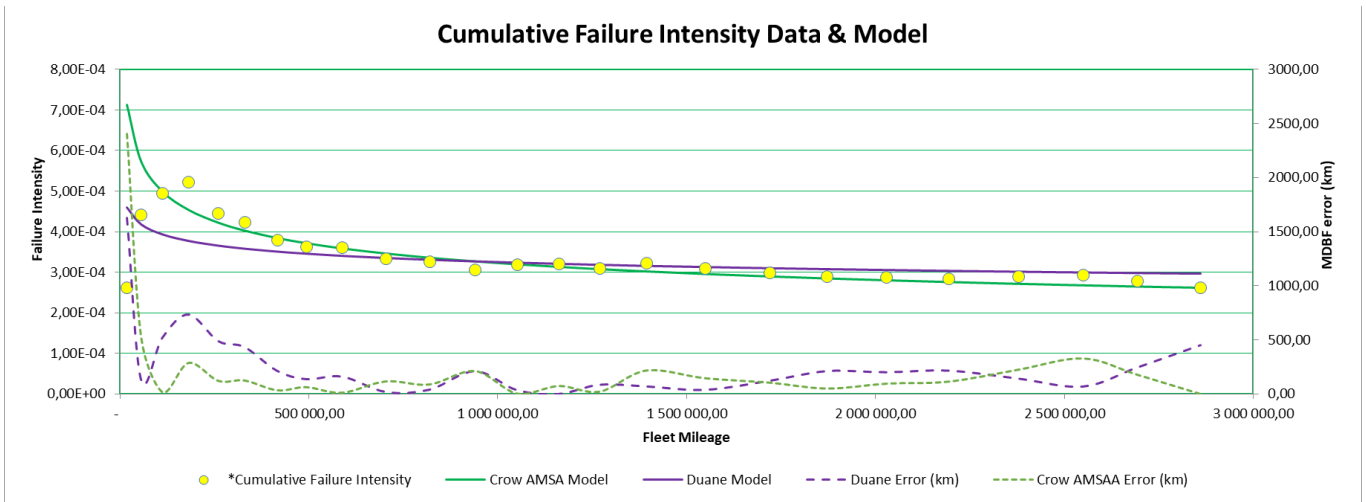


Fig. 6. Metro 1 : Example of Fitting Performances with Crow-AMSAA and Duane algorithms

151  
 152  
 153 VI. ASSESS THE RELIABILITY WITH A REFERENCE PROFILE

154 Once  $(\beta_i, \lambda_{0i})$  parameters are estimated with (i) the number of projects selected as similar and relevant for the scope of the  
 155 study (2 in our example), it becomes possible to calculate or plot dedicate curves with any fleet mileage (different from the  
 156 original ones by using the one for a new tender for example) or to have a direct analytical estimation (1). Indeed  $(\beta_i, \lambda_{0i})$  are  
 157 independent from the original fleet mileage. They represent the product reliability and also the company's efforts to reach that  
 158 level of performance. The more effort is done the more  $\beta_i$  is close to 0.

159 So the projection done in another operational profile assume that the initial reliability  $\lambda_{0i}$  have the same order of magnitude  
 160 and that the company's effort  $\beta_i$  will be the same. Those conditions are explicitly mentioned to the tender team. In case of the fleet  
 161 mileage is too low (for example if the steady state is not reached or with censored data) or the representativeness of the data is  
 162 not ensured, we can also calculate the confidence bounds. In the illustration it is not necessary.

163 To make a comparison we can choose the same mission profile for two metros. Thus we can select a controlled and Reference  
 164 profile. For this we can use a typical metro profile (10 000 km/month for example) or select according to a specific customer  
 165 hypothesis which is interesting for new tender. In our example let's assume that the expected optimal reliability will be reached  
 166 after 7 Millions km.

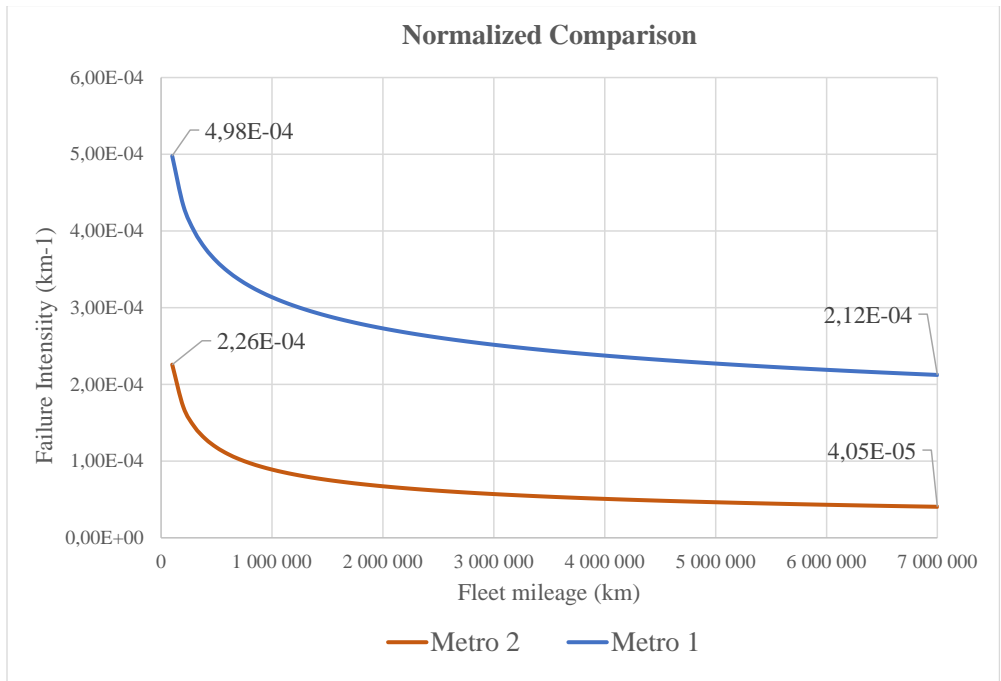


Fig. 7. Performance comparison with a reference mileage profile

167  
 168  
 169 These curves confirm that Metro 2 outperforms Metro 1 over a distance of 7 million km, despite their respective reliability  
 170 growths. Notably, Metro 1 exhibits superior initial performance and reaches its steady state more rapidly than Metro 2. Utilizing  
 171 these curves to evaluate both optimal and intermediate performances is particularly useful, as these metrics can significantly  
 172

173 impact contractual agreements with customers. When assessing optimal performance and the timeline to achieve it, it becomes  
 174 clear that the average failure rate is not an appropriate KPI for either metro.

175 Furthermore, the direct comparison indicates the smallest performance gap between Metro 2 and Metro 1 is 26%, implying  
 176 that Metro 2's performance does not exceed 26% of Metro 1's. However, under this standardized mission profile, the gap narrows  
 177 to 19%. This suggests that when evaluated under reference conditions, the discrepancy is greater than initially observed through  
 178 direct comparison.

## 179 VII. AVERAGE SPEED CORRECTION

180 With the previous step we have compared the performances as if both fleet were running in a same mileage condition.  
 181 Similarly it is possible to use the time in operation or powered up time as a reference x axis. Another option is to make a focus  
 182 on a given subsystem. If the method is applied with mileage as basis time can be used also depending on the need.

183 Indeed in the railway industry and for the rolling stock, the reliability target is usually allocated by the customer in term of  
 184 failure intensity. The target is a fixed value for a given time T (for example end of the fleet delivery + x months). This can be  
 185 formalized in (10).

$$186 \quad \text{Failure intensity Target}_{Fleet}(T) = \frac{\text{Total Number of failures observed within the Fleet}(T)}{\text{Cumulated Fleet Mileage}(T)} \quad (10)$$

187  
 188 The underlying assumption is that the failure intensity is constant in time which is not the case on the real field conditions.  
 189 This is a simplification for the specification. In project condition this target is check against field estimation. From (10) one can  
 190 link the cumulated fleet mileage with the average speed and T cumulated operating time:

$$191 \quad \text{Failure intensity Target}_{Fleet}(T) = \frac{\text{Total Number of failures observed within the Fleet}}{\text{Average Speed}_{Fleet} * T} \quad (11)$$

192  
 193 This simple calculation shows that the Failure intensity depends on the total mileage and then also to the average speed. The  
 194 Average speed can be considered as a critical factor in fleet operations, varying widely among customers due to differences in  
 195 timetables, track lengths, number of stations, and other factors. As indicated by (11), it significantly influences failure intensity.  
 196 Therefore, it become possible to correct prediction considering the varying average speeds.

197 Let's take an example; assume that we want to predict the performance for a new product for a tender during a T period with  
 198 an average speed of 35 km/h given by the customer in the contract. However, the best similar project with REX had an 27 km/h  
 199 average speed. By having a higher average speed and knowing that failure occurrences are mainly time base, we can deduce that  
 200 the performance of the new project will be higher than the old one for the same timeframe. So the problem is what would be the  
 201 performance of the new project considering the "new" average speed is at 35 km/h and knowing that the REX is at 27 km/h?

202 Analogous to adjusting for fleet mileage, we recommend calculating the failure intensity as if both fleets operated at a uniform  
 203 average speed—a reference average speed. This approach is formalized in equation (5).

$$204 \quad \text{Failure intensity Corrected}_{Fleet}(T) = \frac{\text{Total Number of failures observed within the Fleet}}{\text{Average Speed}_{Normalized} * T} \quad (12)$$

205 Calculated with (11):

$$206 \quad \text{Failure intensity Corrected}_{Fleet}(T) = \frac{\text{Average Speed}}{\text{Average Speed}_{Normalized}} * \text{Failure intensity}_{Fleet}(T) \quad (13)$$

207 For our example for tender it comes:

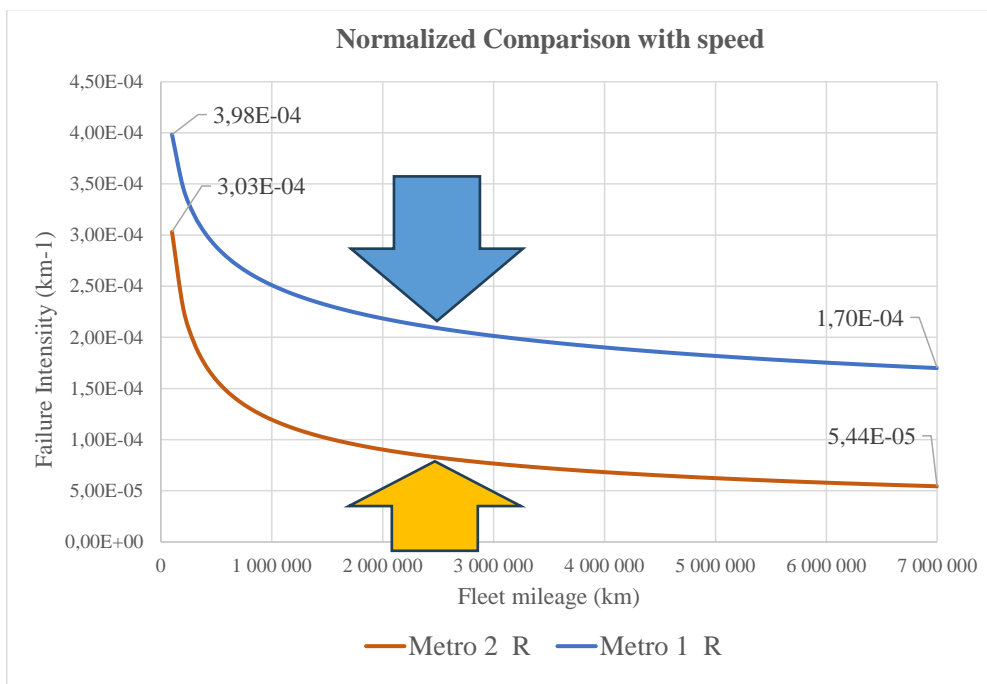
$$208 \quad \text{Failure intensity Corrected}_{Fleet}(T) = \frac{27(DEX)}{35(Target)} * \text{Model}_{Fleet}(T) \quad (14)$$

209 In this case we apply the target speed of a new project to a given REX, but it not the only application for your proposal. the  
 210 original need is to compare respective performances. Let's apply this correction to the first comparison example, which is  
 211 particularly notable due to the significant difference in speeds. Metro 2 operates on a long track with a substantial distance  
 212 between two stations, unlike Metro 1. Consequently, Metro 2 has an average speed of 47 km/h, while Metro 1's average speed is  
 213 only 28 km/h. We will conduct an analysis assuming an average speed of 35 km/h for both metros (35 km/h is the average speed  
 214 set by the platform as key assumption). For each project (i) we plot (15)

$$215 \quad \text{Model Corrected}_{Fleet i}(T) = \frac{\text{Average Speed}(i)}{35} * \text{Model}_{Fleet i}(T) \quad (15)$$

216

217 This correction results are in the following graph:



218  
219 Fig. 8. Comparison with corrected an reference Average Speed

220 By doing this correction the gap between Metro 1 and 2 is reduced and goes to 32% : Metro 1 reaches at best 32% of Metro  
221 2 Failure intensity. Mathematically it is formalized in (16)

$$222 \text{Cumulated Failure Intensity Corrected}_{Fleet i} (\text{Cumulated km})$$

$$223 = \lambda 0i Rex * \frac{\text{Average Speed}(i)}{35} * (\text{Cumulated km})^{\beta i-1} \quad (16)$$

224 In other words the speed correction change the scale parameter  $\lambda 0$  (17):

$$225 \lambda 0i \text{ Corrected} = \lambda 0i Rex * \frac{\text{Average Speed}(i)}{\text{Average Speed}_{Nomalized}} \quad (17)$$

226 The shape parameter  $\beta$  is not affected by the speed considering that it rely on the process performance to detect and fix the  
227 systematic issues in the product.

228  
229 VIII. RESULTS

230 This method is allowing the RAM Engineer to get the Rolling Stock performances in the same conditions for mileage and  
231 speed.

232 Then, the remaining gaps are due to certain customer sensitivity (customers are more or less demanding in term off  
233 performances), or the climate, or the product itself: the way it was designed and manufactured but also the operational or  
234 maintenance practices.

235 This is the starting point of a qualitative analysis which is looking for the root causes of those differences. This analysis shall  
236 be done with the warranty teams of each project to understand their difficulties, their organization, their good practices and lesson  
237 learnt. A multi project analysis is able to find common weaknesses and strengths and push a platform evolutions.

238 IX. DISCUSSION AND OPEN POINTS

239 It should be understood that this comparison does not determine which product is superior in absolute terms. Rather, it aims  
240 to correct for biases introduced by differing mission profiles. The key assumption is that the failure occurrence is mainly time  
241 based which is actually the case for almost all embedded devices (except for bogie). We can also face an issue in term of lack of  
242 data representativeness, or censored data, of, for example, a reduce period of observation. In this case both parameters might be  
243 affected that why we recommend to use confidence bounds.

244 Another limitation for this method does not account for other significant factors such as product architecture, customer  
245 expectations, climatic conditions, or variations in manufacturing and maintenance practices. A critical aspect is product  
246 architecture; for instance, metros can range from 2-car to 9-car configurations, each with differing numbers of subsystems like  
247 traction, braking systems, auxiliary power supplies, and air conditioning units. Comparing products with significant architectural  
248 differences—such as between a 2-car and a 9-car metro—might misleadingly suggest the larger is less reliable due to its



249 complexity. This methodology attempts to mitigate such bias during the initial scope definition and selection process. However,  
250 there are instances where a direct comparison is challenging due to the lack of comparable field data. In our analysis, comparing  
251 a 5-car to a 6-car metro assumes a level of comparability that may not exist in practice, potentially leading to inaccurate  
252 conclusions about reliability. Therefore, an ideal next step involves refining the methodology to better estimate and adjust for  
253 architectural biases.

254 .

## 255 X. CONCLUSION

256 The methodology offers a structured approach to comparing the reliability performances of various rolling stocks,  
257 acknowledging that they operate under diverse conditions, such as differing numbers of trains, total mileage, and operating times.  
258 In the railway industry, identical mission profiles for two distinct fleets are highly improbable due to variations in infrastructure  
259 and schedules. Direct comparisons, therefore, lack the robustness needed for accurate gap measurement. Our proposed method  
260 involves comparing performance within a standardized mission profile, necessitating Reliability Growth (RG) modelling to  
261 simulate conditions of equal mileage and speed for all subjects. The preference for the Crow AMSAA model is due to its  
262 effectiveness in fitting data towards the observation's end, providing insights into the potential optimal performance against set  
263 contractual targets. This methodology lays the groundwork for a qualitative analysis (not covered here) aimed at identifying best  
264 practices and revealing specific products' strengths and weaknesses by first quantifying performance before exploring underlying  
265 causes.

266

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272

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